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Representation-theoretic and combinatorial structure of moduli spaces, e.g.:

- Quantum groups actions on cohomology/K-theory of moduli spaces
- Enumerative invariants particularly K-theoretic (Donaldson-Thomas-type) invariants

Key example:  $\mathrm{Hilb}_n(S)$  (and tautological bundle  $\mathcal{O}^{[n]}$ )



For example, computing two limits of the K-theoretic DT partition function of a particular threefold, we deduce:

$$\frac{\displaystyle\sum_{m,n\geq 0}^{\infty}\chi\left(\mathrm{Hilb}_{n}\mathbb{C}^{2},\bar{S}^{m}(\mathcal{O}^{[n]})\right)y^{m}q^{n}}{\mathsf{same with }y=0}$$

is symmetric under  $q \leftrightarrow y$ .

- Other geometric/physical/representation-theoretic interpretations of above result
- ▶ Other moduli of sheaves/tautological classes, other invariants  $(\chi_y$ -genera, elliptic genera)
- ► K-theoretic DT/stable pairs correspondence & relation with quantum K-theory
- ► K-theoretic DT invariants <sup>?</sup> refined/motivic DT invariants