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on leave from Harvard U.

<i>Physics</i>	<i>Geometry</i>	<i>Rep. Theory</i>
0d, 1d IM	Symplectic/Poisson	$U(\mathfrak{g})$
2d CFT	Hyperbolic/Teichmuller	$U(\hat{\mathfrak{g}}), \mathcal{W}(\mathfrak{g})$
3d TQFT	Topology	$U_q(\mathfrak{g}), \text{Skein}$
(4,5,6)d SYM	Algebraic Geometry	$U_q(\hat{\mathfrak{g}}), U_{q,t}(\hat{\mathfrak{g}})$

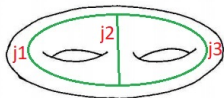


Macdonald polynomials  $P_j(x)$  with parameters  $q, t$

Evaluation:  $x = t^{\frac{1}{2}}$  special point,  $P_i\left(t^{\frac{1}{2}}\right)$  factorizes

Symmetry:  $P_j\left(t^{\frac{1}{2}}q^{\frac{i}{2}}\right)$  w.r.t. exchange  $(i, j)$

Modularity: provide  $SL(2, \mathbb{Z}) \simeq MCG(\Sigma_1)$  representations



Polynomials  $P_{j_1, j_2, j_3}(x_{12}, x_{13}, x_{23})$  with parameters  $q, t$

Evaluation:  $\checkmark$  Symmetry:  $\checkmark$  Modularity:  $\checkmark$   $MCG(\Sigma_2)$