



# Once in a Decade Opportunity to Address Gerrymandering

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Somersille Math Education Services

# Outline

- I. The problem: Gerrymandering
  
- II. The New Metric: Geography and Election Outcome (GEO) metric to measure gerrymandering  
Marion Campisi, Thomas Ratliff, SS, Ellen Veomett
  
- III. “Out of the box ideas”
  - Other (Better?) Voting Methods that don’t involve districting
  - Voting Rights Lawsuit Example

Problem: Extreme Gerrymandering

Opportunity:



# May 2021: Census results released

13 states gained or lost a seat

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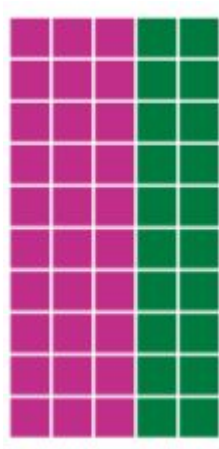
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Montana 2 Seats (+1)      West VA 2 Seats (-1)

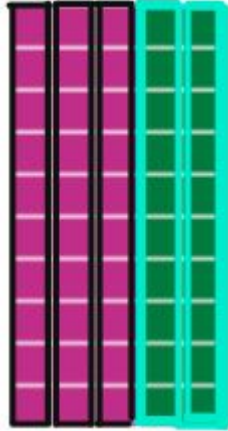


# Districting



50 voters to be divided into 5 districts of 10 people each

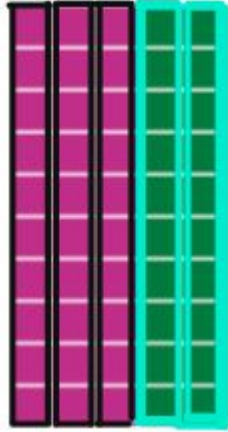
# Proportional Maps



3 pink districts

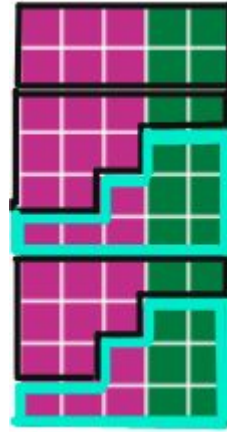
2 green districts

# Proportional Maps



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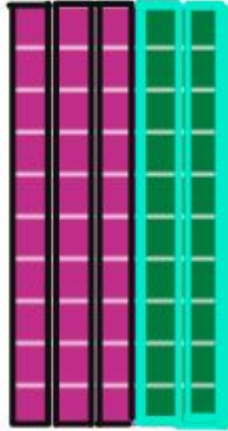
2 green



3 pink

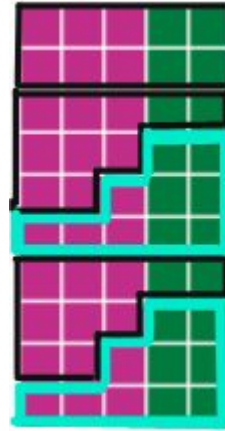
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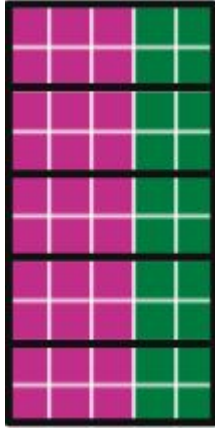
\*There's no rule that maps need to be proportional

Just Equal Population



# Non Proportional Maps

**Cracking**



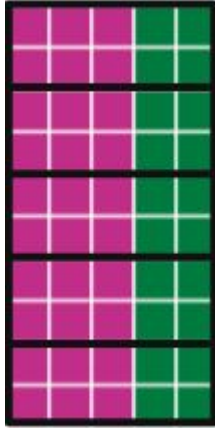
5 pink

0 green

Pink wins all

# Non Proportional Maps

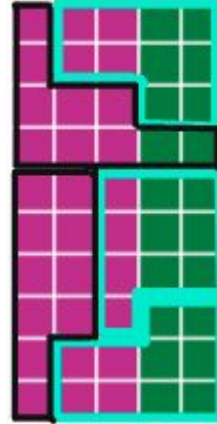
Cracking



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Pink wins all



2 pink

3 green

Green wins majority

Packing and  
Cracking

History: 1812 Gov Elbridge Gerry



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\*Gerrymander

# Is it Illegal?

In the 20th century and afterwards, federal courts have deemed extreme cases of gerrymandering to be unconstitutional but have struggled with how to define the types of gerrymandering

# Is this Illegal?

Voting Rights Act 1965 “prohibits racial discrimination in voting”.

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Preventing 2 types of discrimination

**Vote Denial:** Bans voting qualifications or prerequisites to vote based on color.

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Preventing 2 types of discrimination

**Vote Denial:** Bans voting qualifications or prerequisites to vote based on color.

**Vote Dilution:** Dilute the effectiveness of one’s vote. Prevent racial minorities from electing their preferred candidates.

# Thornburg v. Gingles 1986

Gingles Conditions For Voting Rights Lawsuit Claims

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Compactness:

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### Racially Polarized Voting:

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- 2) Minority Groups must be politically cohesive (Vote similarly. As a bloc)
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**Remedy for VRA lawsuits: Draw Majority Minority Districts**

# “Crimes Against Geography”

North Carolina

1st District



4th District



12th District



# “Crimes Against Geography”

Maryland’s 3rd District

“The Praying Mantis”



# “Crimes Against Geography”

Texas

33rd District



35th District

“Upside Down Elephant”



# “Crimes Against Geography”

Pennsylvania 7th District

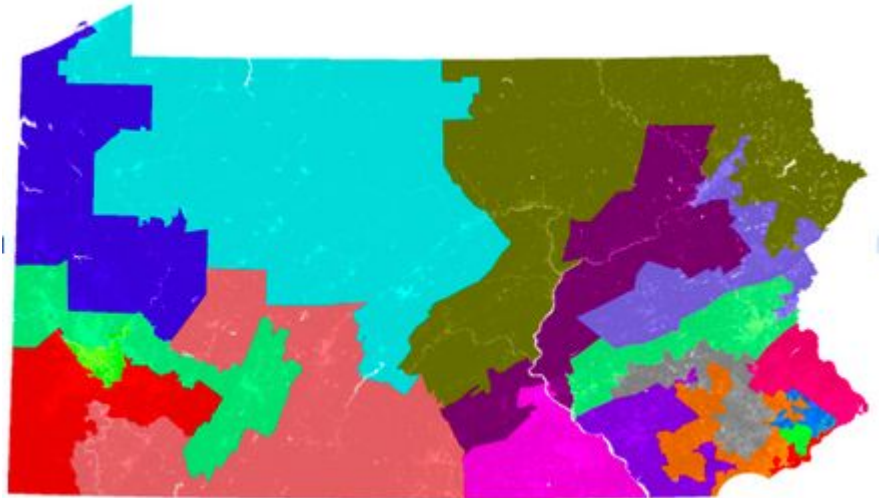
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# Why it's so problematic

Politicians choosing their voters

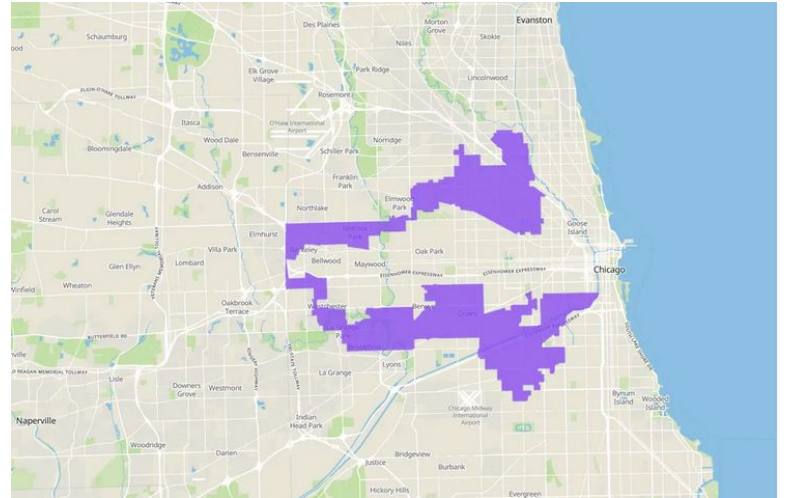
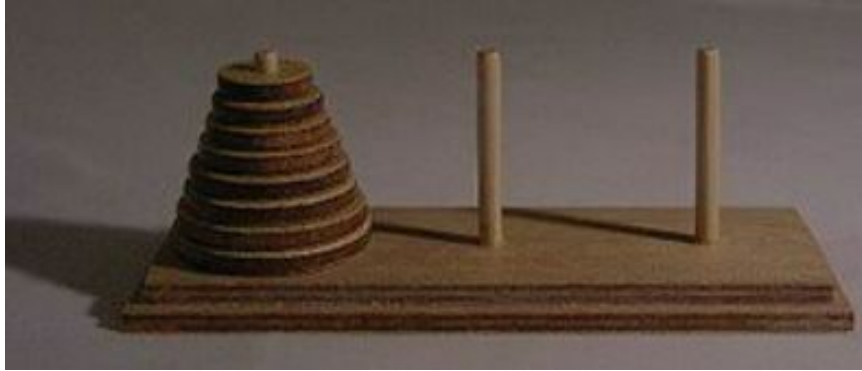
Vs.

Voters choosing their elected officials





# Why I Got Involved In Redistricting



# Stages of Awakening

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These are people!
- 4) Turns out fair is a subjective notion. It's an over-constrained problem

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Needed team building, coalitions, allies. Community members, Politicians, Lawyers and lawmakers, Social Scientists, as well as Mathematicians...

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Needed team building, coalitions, allies. Community members, Politicians, Lawyers and lawmakers, Social Scientists, as well as Mathematicians...

All types of mathematicians



Bring your brand of math to the problem



# Opportunity:

Measuring Gerrymandering

# Currently Popular Metrics

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Map Data (Compactness)

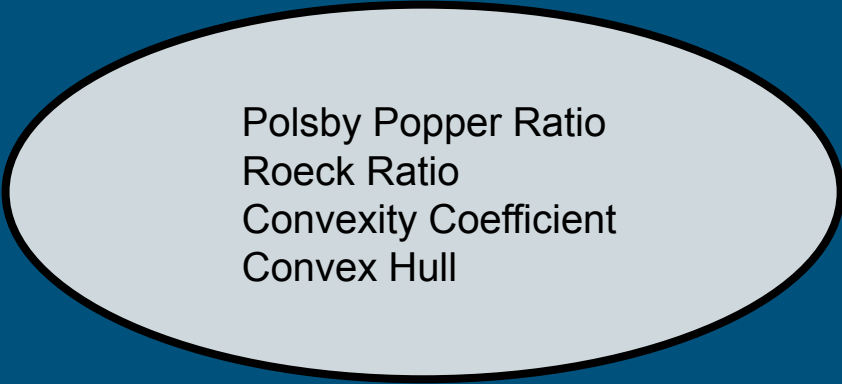
Election Data

# Currently Popular Metrics

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Map Data (Compactness)

Election Data



- Polsby Popper Ratio
- Roeck Ratio
- Convexity Coefficient
- Convex Hull

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## Map Data (Compactness)

Polsby Popper Ratio  
Roeck Ratio  
Convexity Coefficient  
Convex Hull

## Election Data

Mean Median  
Efficiency Gap  
Partisan Bias  
Declination

# NEW: Geography and Election Outcome Metric

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Map Data (Compactness)

Election Data

Polsby Popper  
Roeck Ratio  
Convexity Coef  
Convex Hull

**GEO Metric**

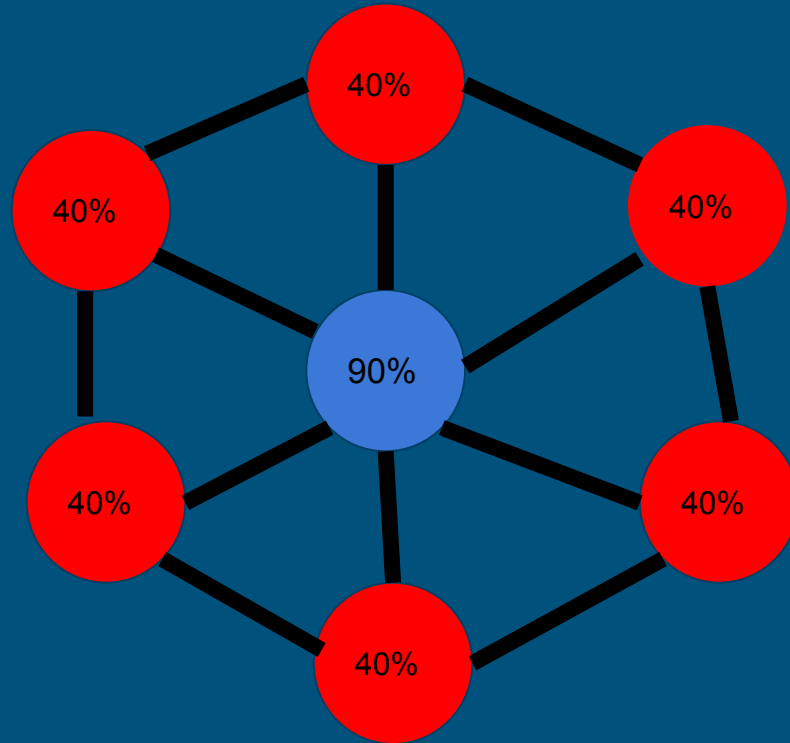
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**Uses Both Map Data and Election Data**

**Marion Campisi, Thomas Ratliff, SS, Ellen Veomett**

# Sample of how GEO measures gerrymandering

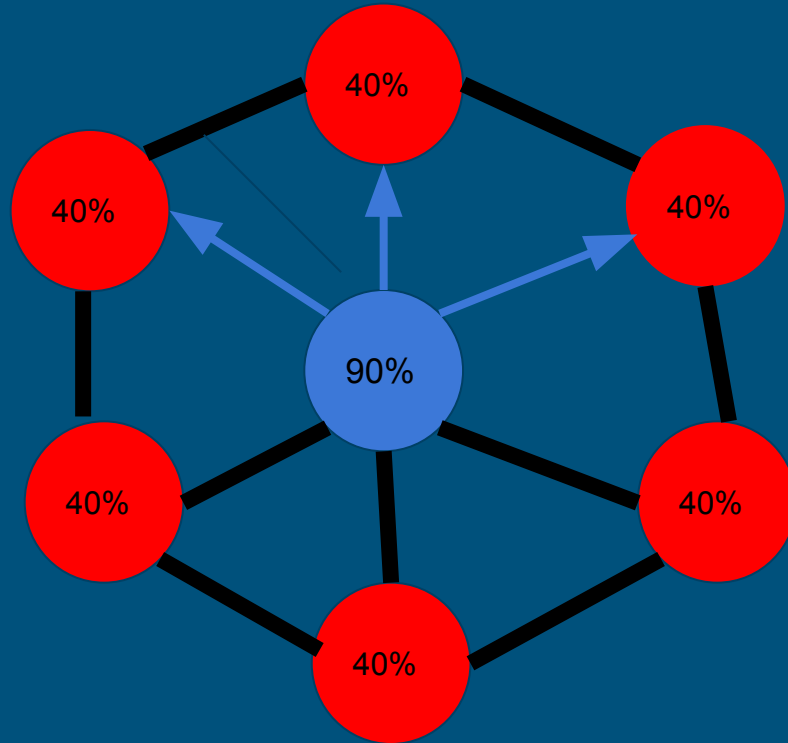
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Percentages of Blue vote share in each district

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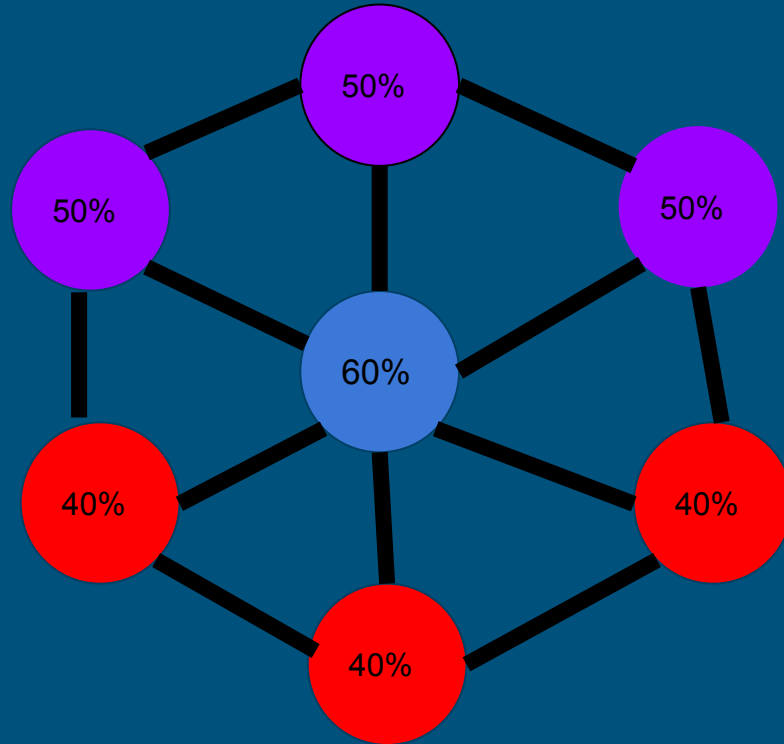
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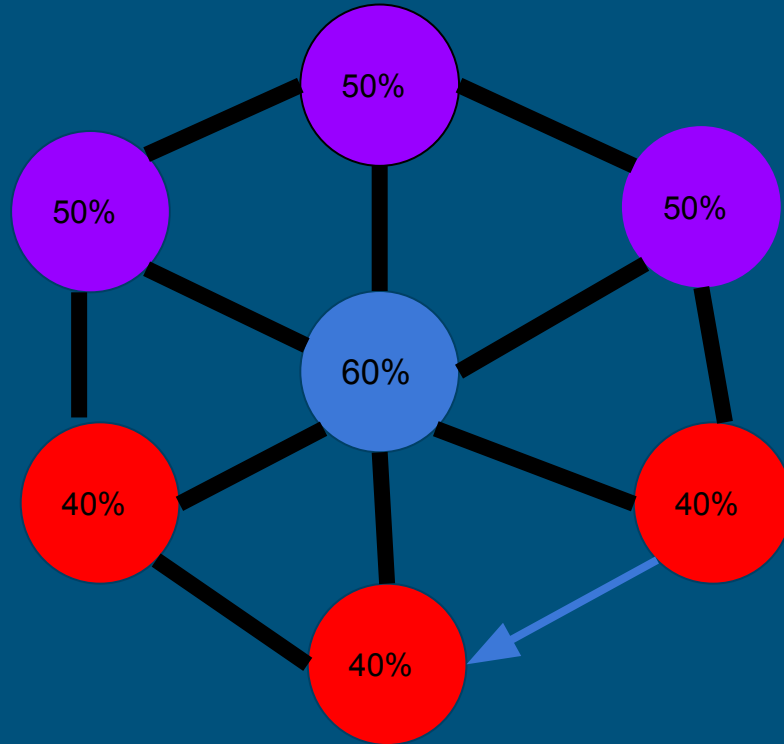
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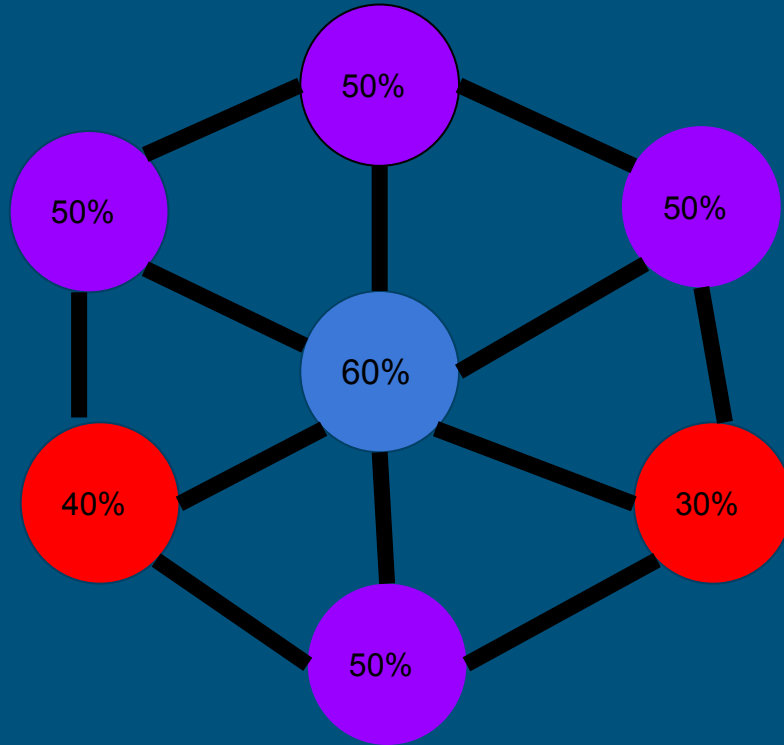
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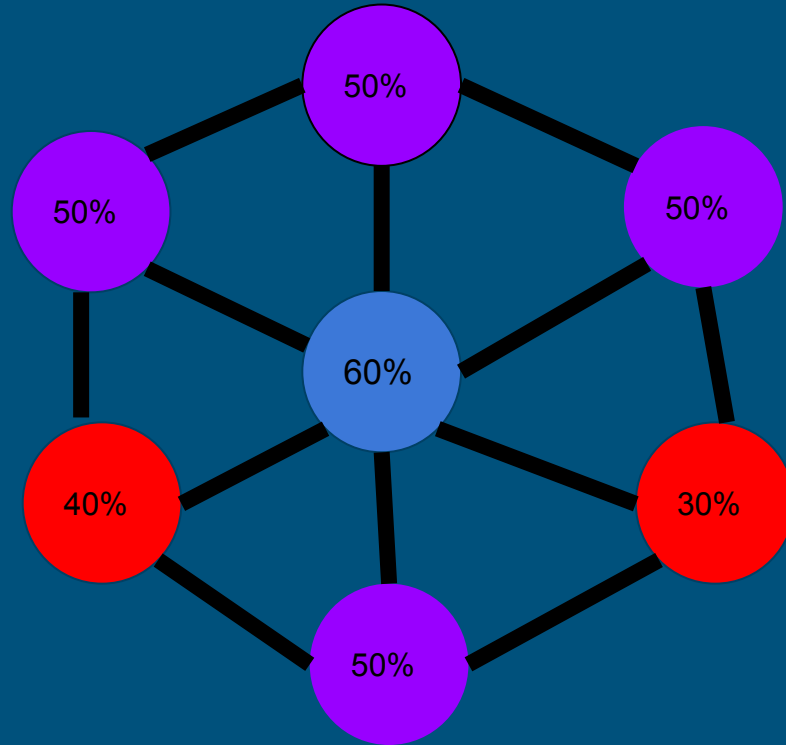
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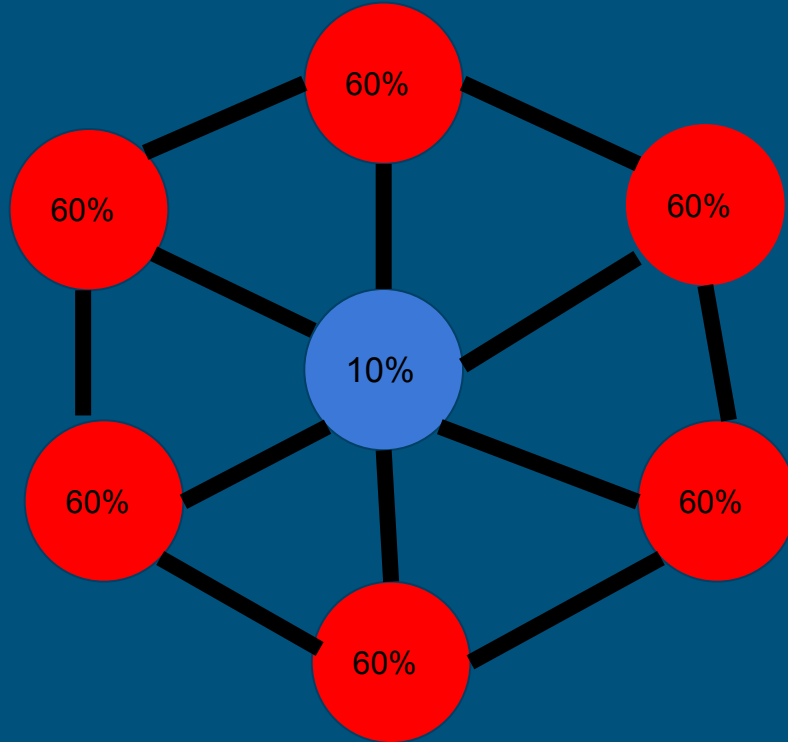
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Blue Party GEO Metric Score 4

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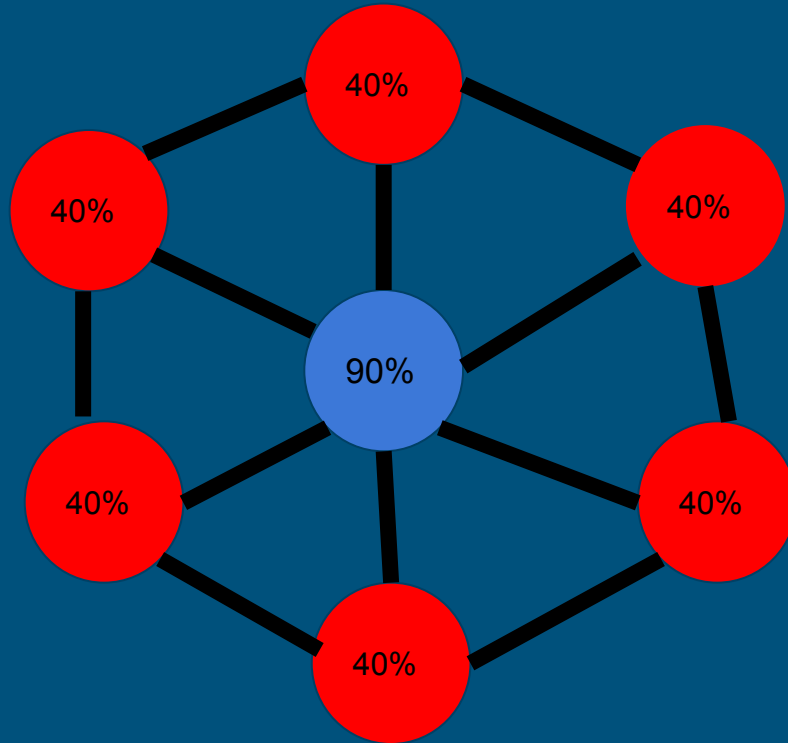


Percentages of Red party vote share in each district

Red Party GEO Metric Score 0

# Sample of how GEO measures gerrymandering

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**Blue Party** GEO Metric Score 4

**Red Party** GEO Metric Score 0

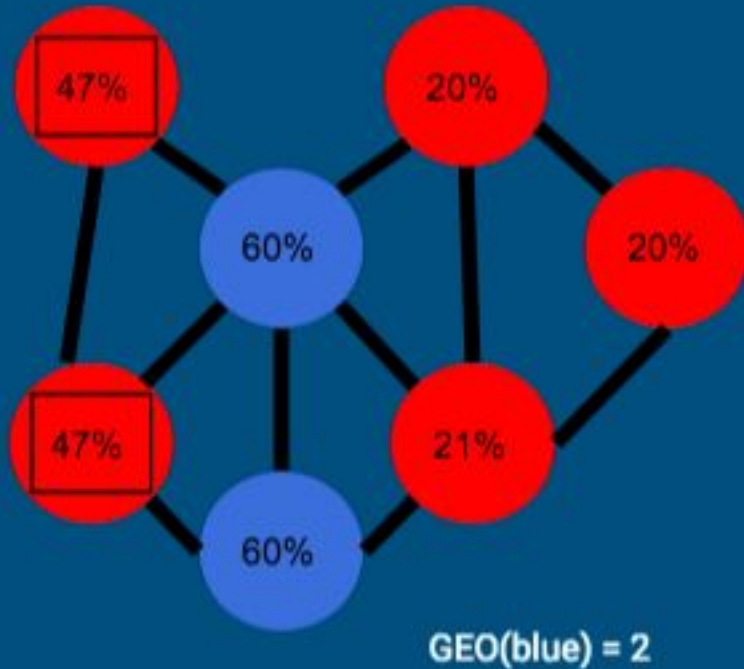
# Why is GEO More Effective?

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Gives two score for the whole District Map - One for each party

Also identifies potentially packed and cracked districts

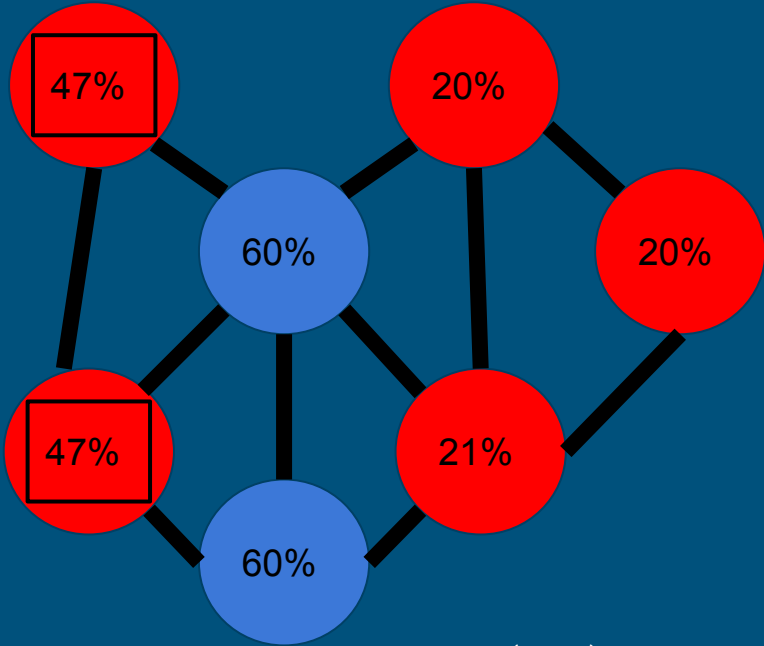
# Why both Geography and Election Outcome Data?



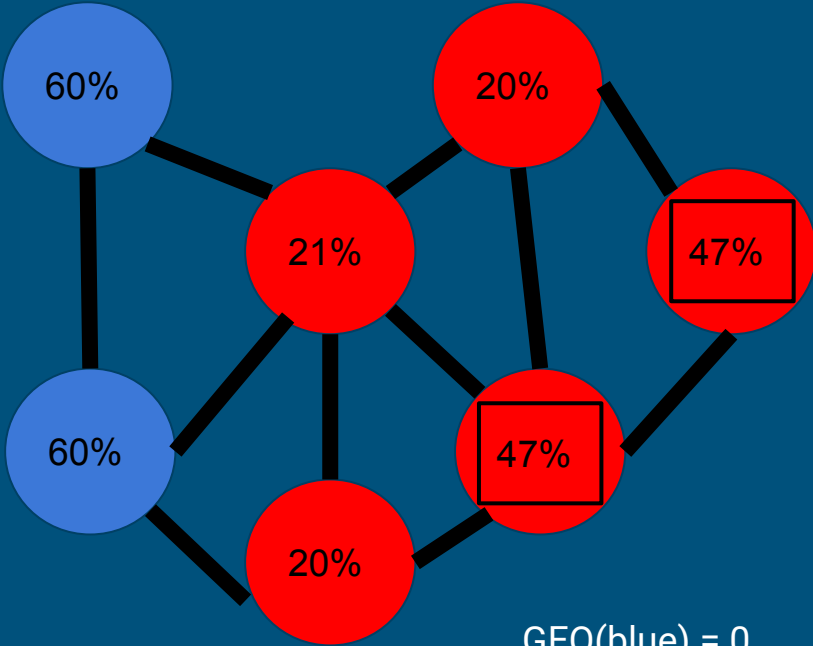


# Why both Geography and Election Outcome data?

Any metric using only Election Outcome can't distinguish between these two maps. But we're more likely to suspect the left one is the result of gerrymandering.



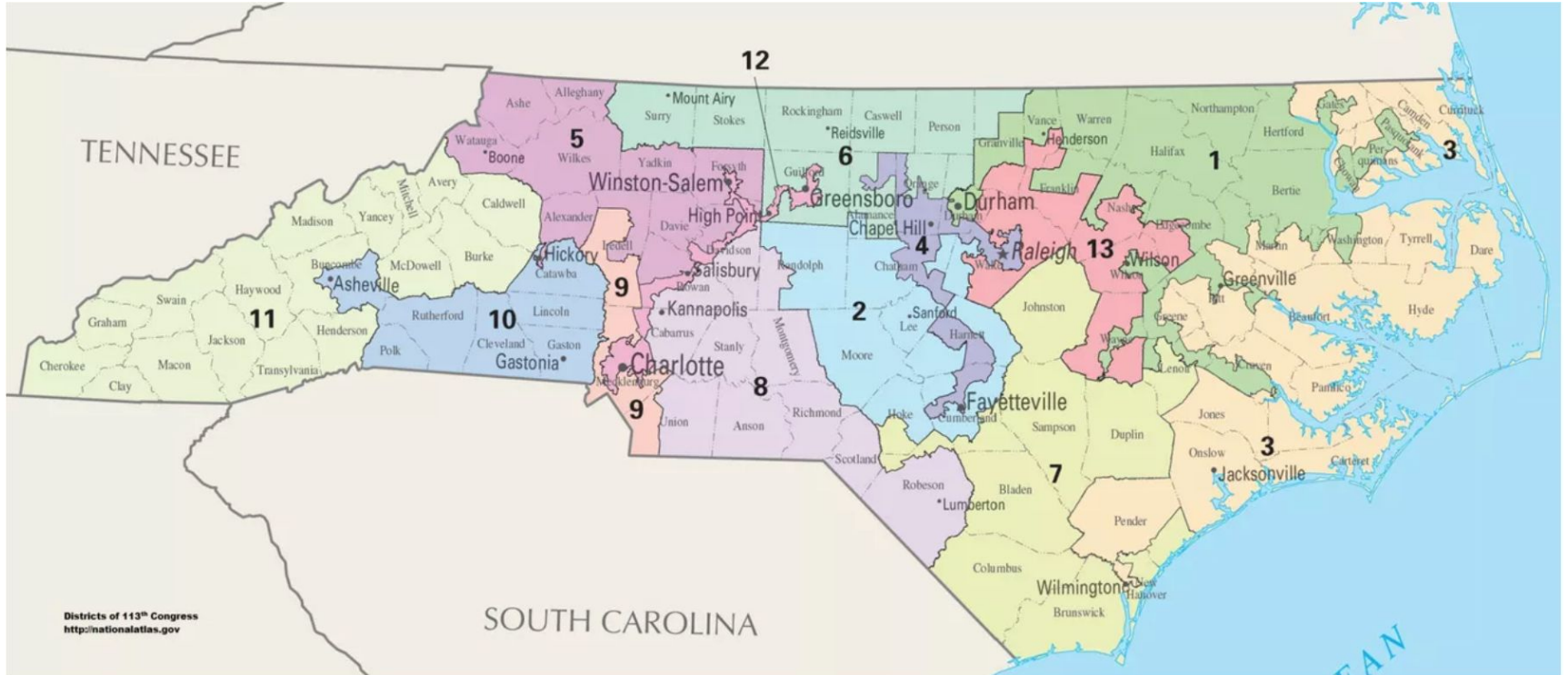
GEO(blue) = 2



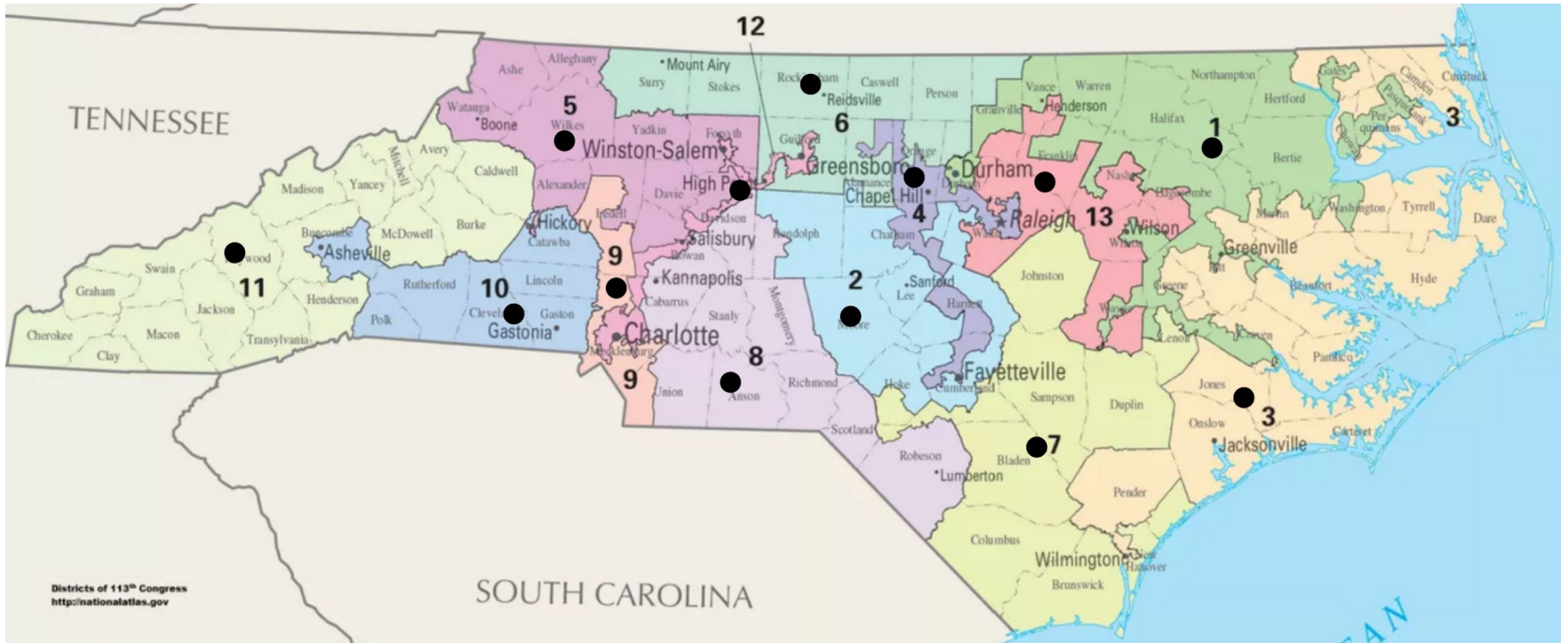
GEO(blue) = 0

# NC

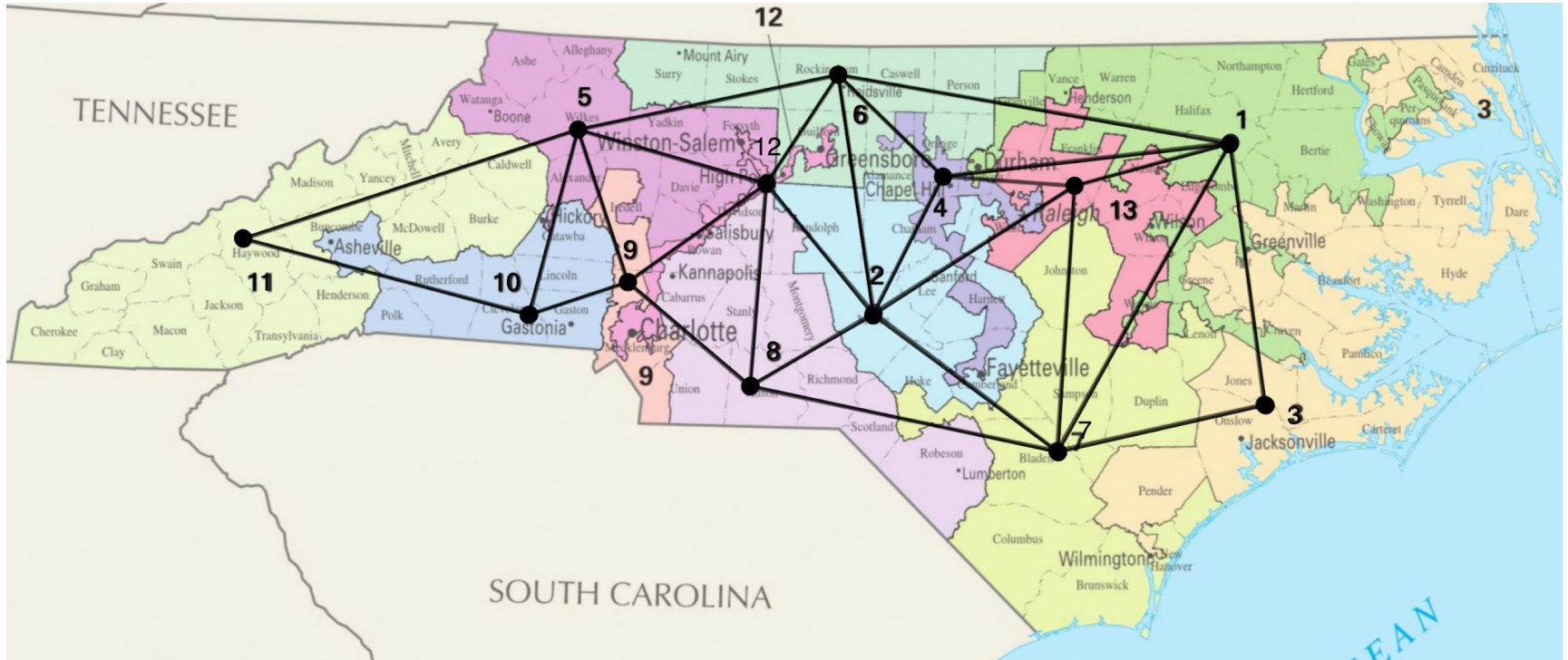
## Start with a map of districts



# Districts turn into vertices

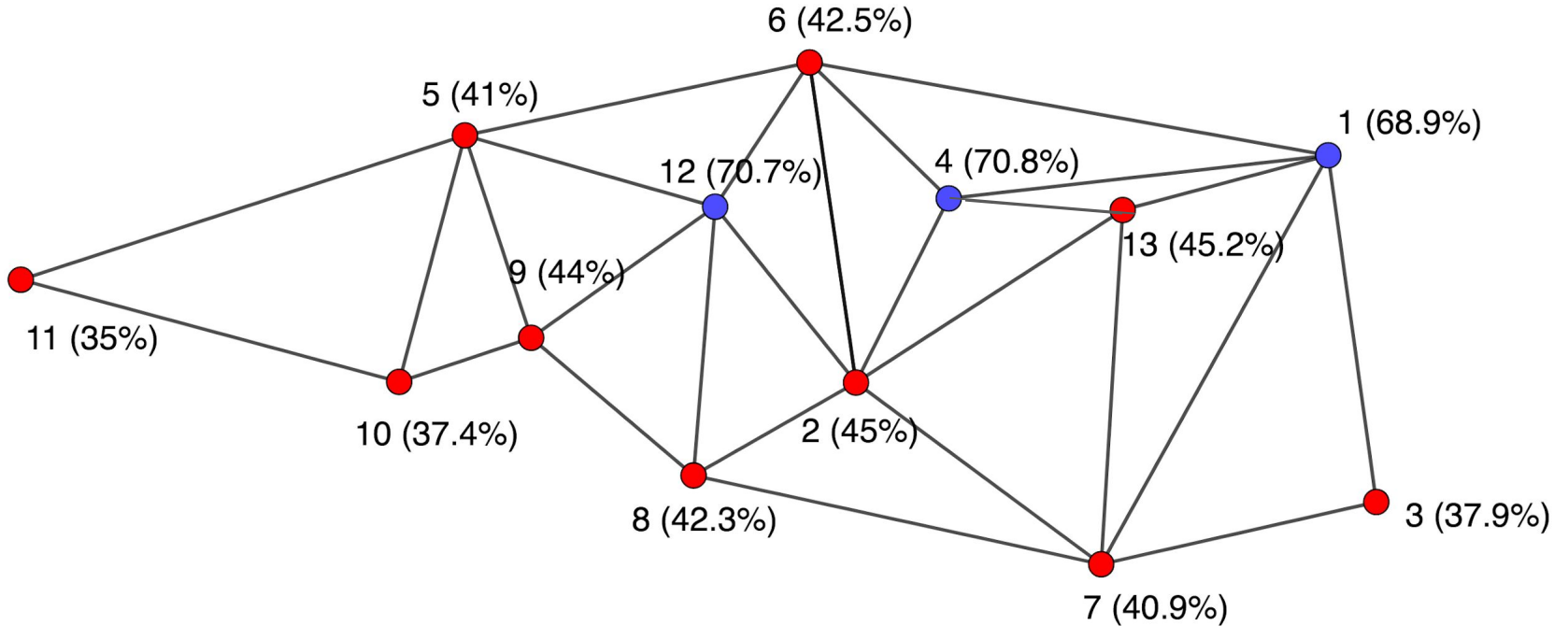


If two districts share a boundary, their corresponding vertices have an edge between them

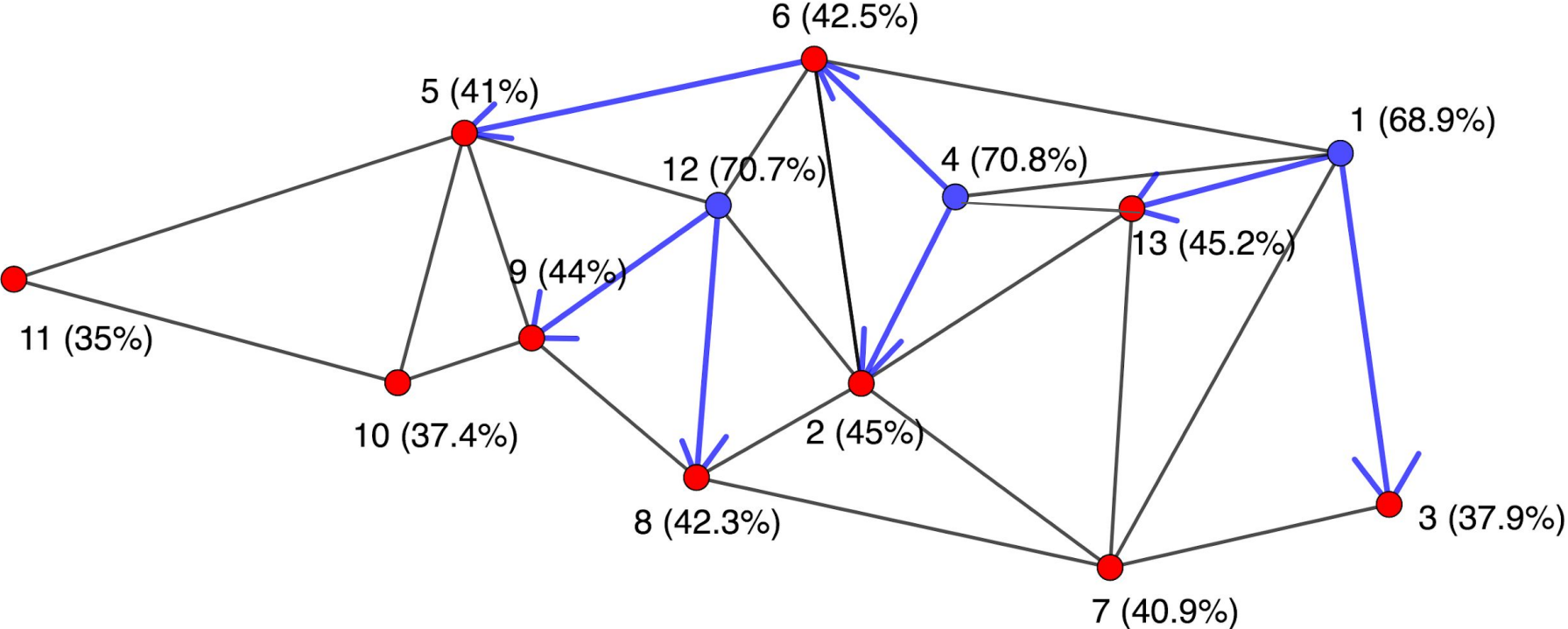


# Big Idea

Votes are exchanged in a reasonable way between districts that share a boundary to see if Dem. party can win more seats

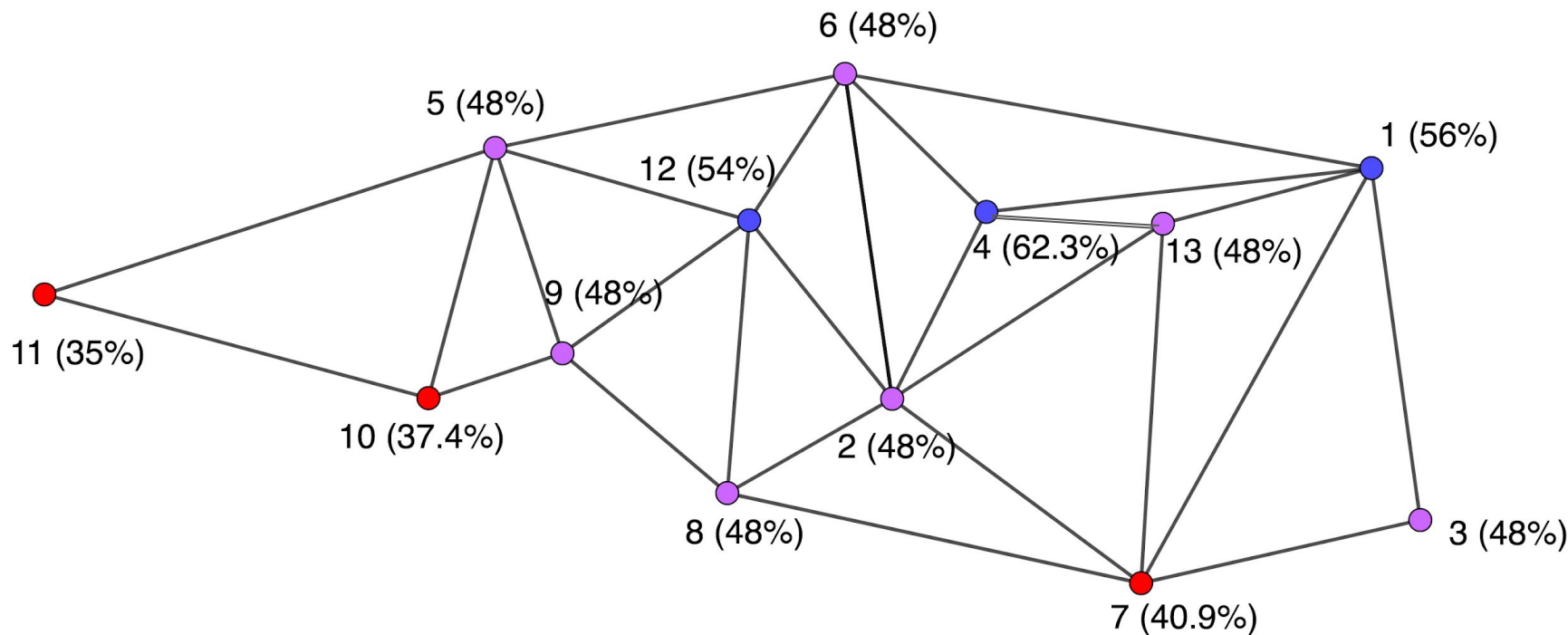


# Potential Vote Movement: Democratic Party



# NC Example

GEO(Dem.) = 7



# Ensembles

Generate tens of thousands or hundreds of thousands of maps

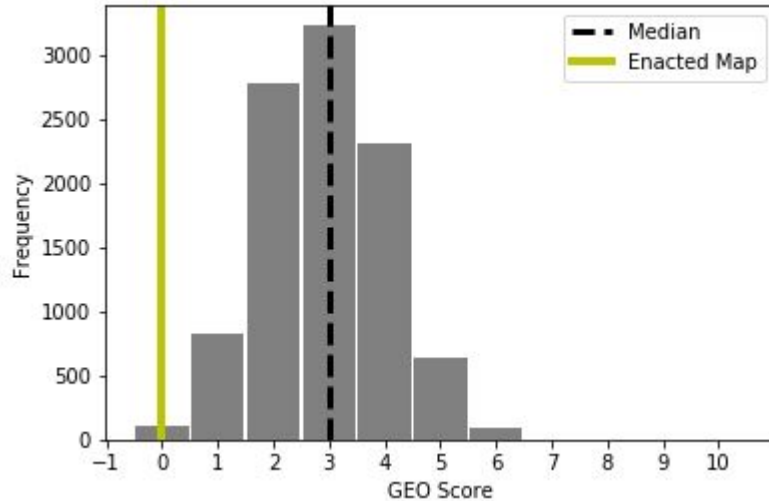
Satisfying conditions

Compare the proposed or enacted map to thousands of “similar” maps.



# GEO Analysis: Pennsylvania Senate Election 2016

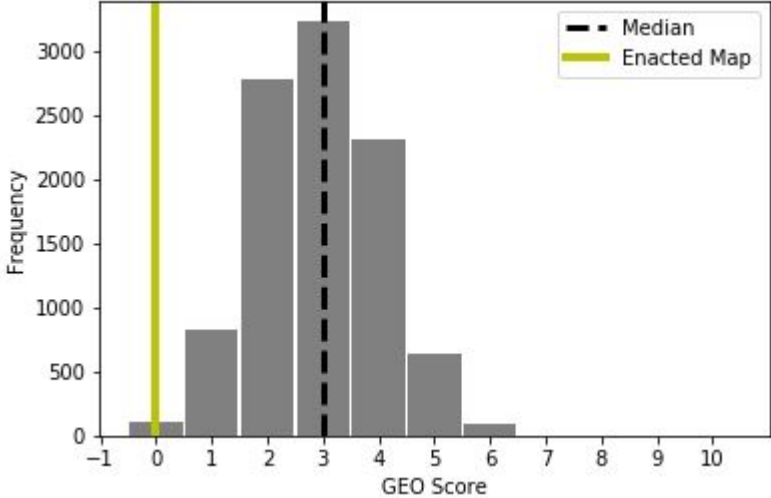
Republican:



Not Possible to Improve Their Outcome

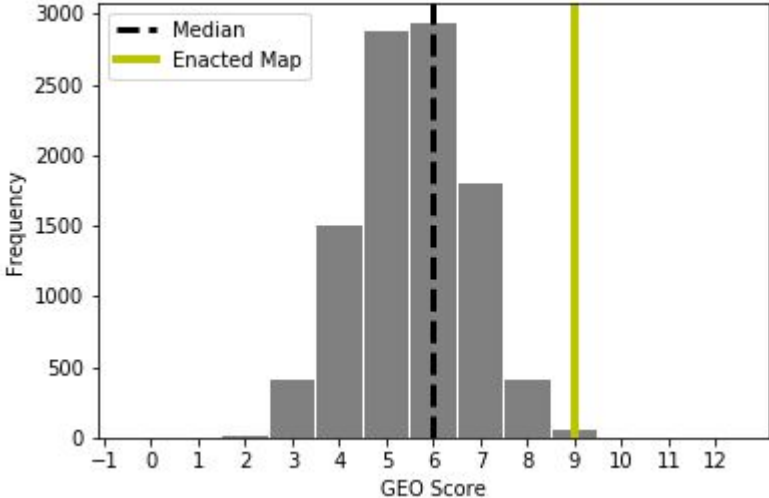
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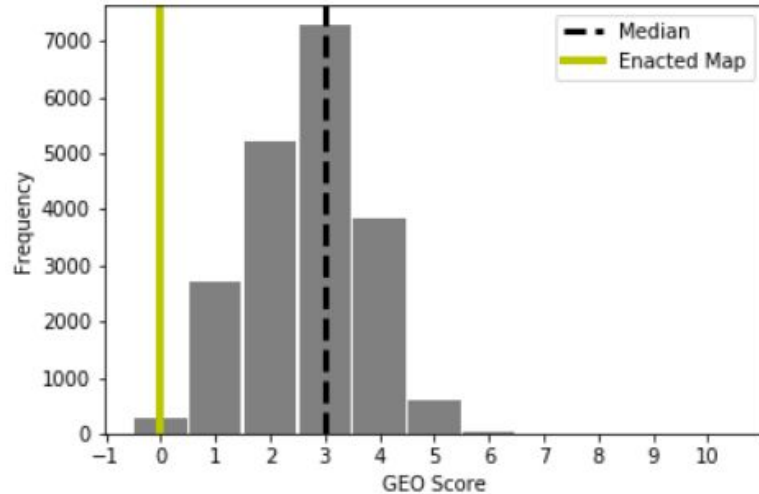
Democrat:



A lot of Potential to Improve Outcome

# GEO Analysis: North Carolina Presidential Election 2016

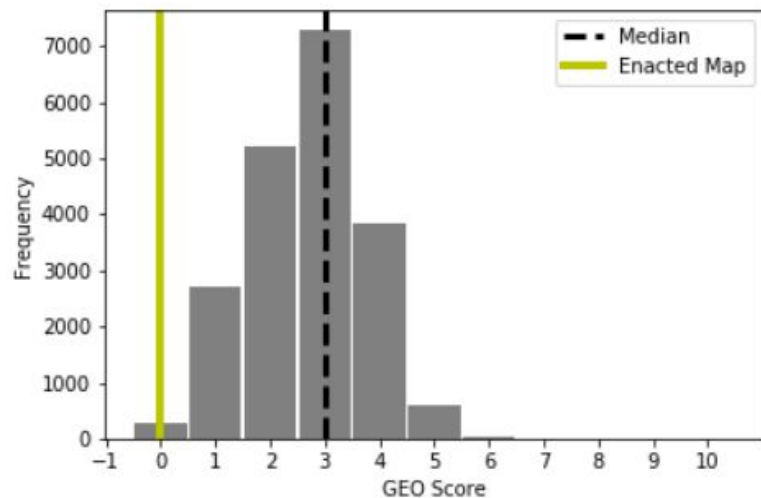
Republican:



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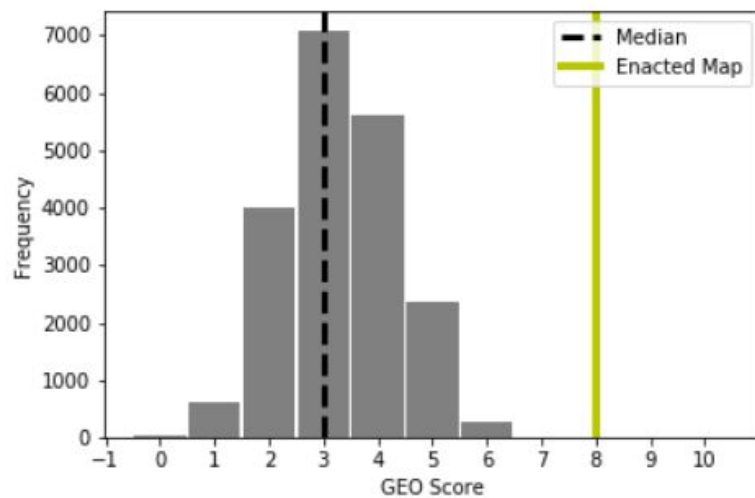
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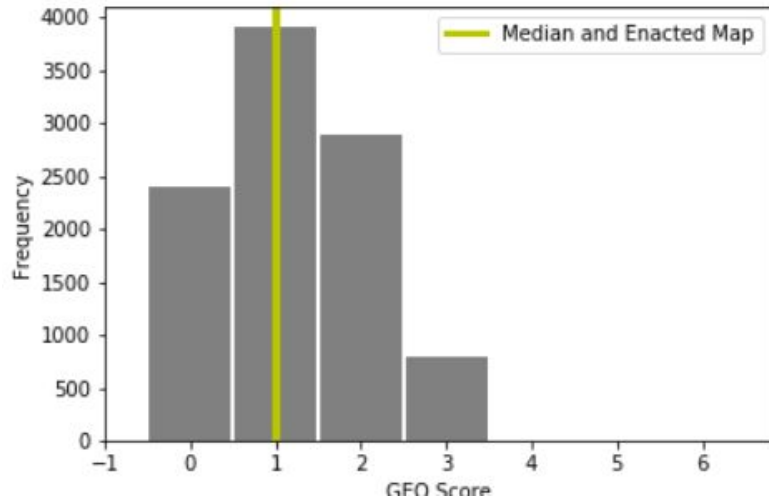
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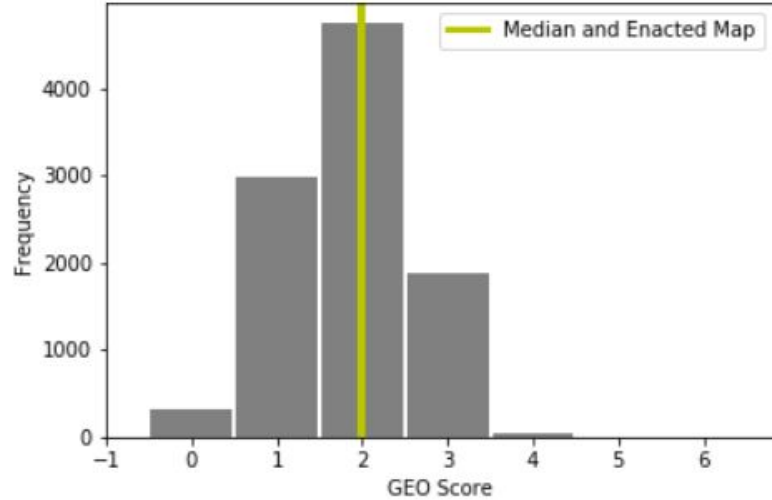
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# CO Gov 2018 - Example a map that is Not Gerrymandered

Republican:



Democrat:



GEO Metric

Fair Redistricting

# Time for Out of the Box Voting Methods

Framers of the Constitution didn't envision an entrenched minority

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Rank Choice Voting : NYC Mayor Democratic Primary

Cumulative Voting: Corporate Boards to preserve minority interests



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Cumulative Voting: Corporate Boards to preserve minority interests

Electoral College:

Only 5 elections in the history of the country where the electoral college outcome is different from the popular vote

2 recently: 2000 and 2016

Only one of the 5 (Bush) ran for re-election and won

# VRA Lawsuit Example: Santa Clara City Council

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Appealed

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Mid 2018 Ballot Measure to split the city into two (3 member) districts and use Rank Choice Voting FAILED

March 2020 Ballot Measure to split the city into Three (2 member) districts FAILED

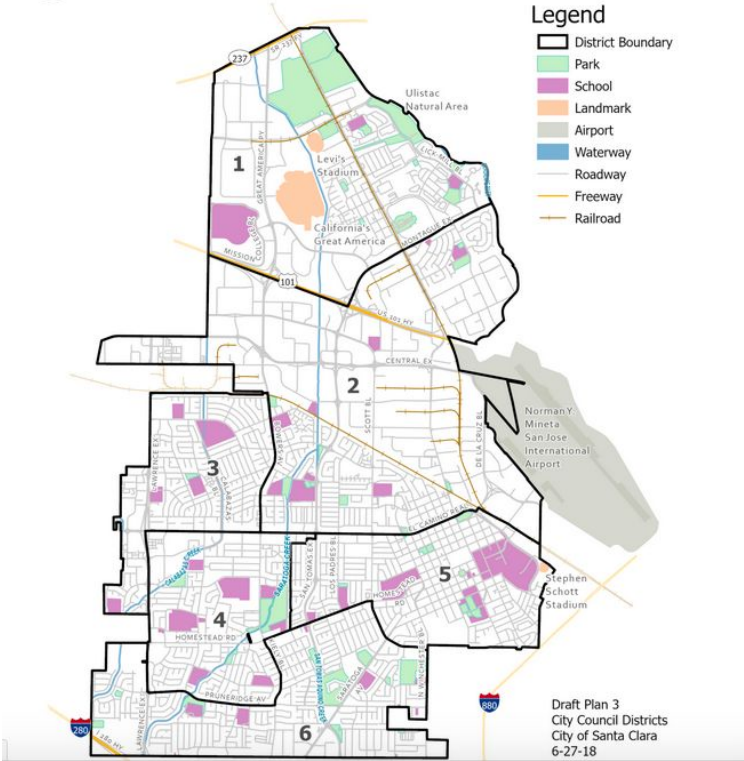
Dec 2020 City lost the last appeal

June 2021 Ballot Measure to make the 6 districts system permanent

# City of Santa Clara



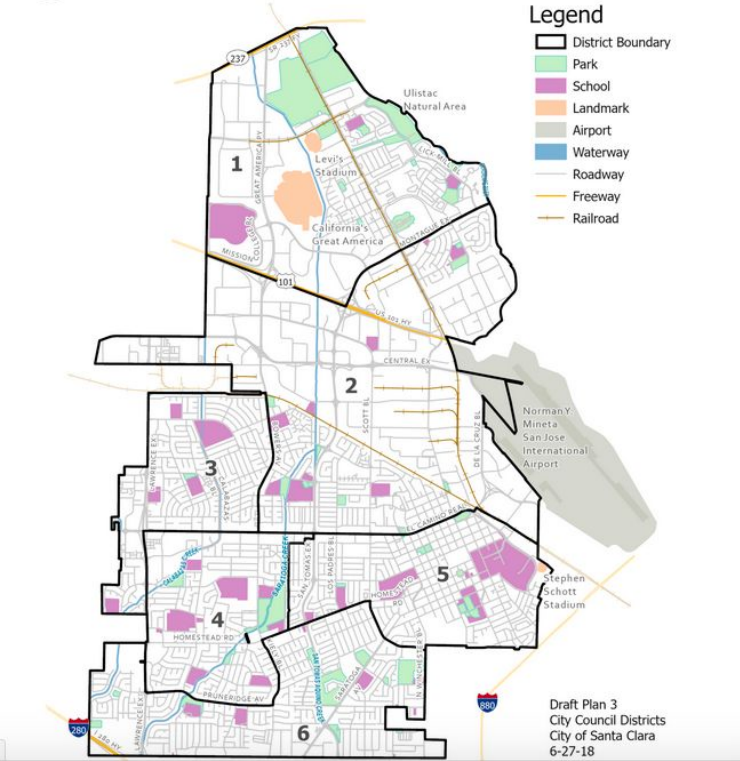
## City of Santa Clara City Council Districts Map



# City of Santa Clara



## City of Santa Clara City Council Districts Map



**Cost: \$6 Million**

# Conclusion

As long as we have districting: The new GEO metric

Maybe it's time we stop relying on others to draw Majority Minority Districts to prevent racial gerrymanders.

# Conclusion

## Potential Research Topics

Racially Polarized Voting

Size of the Space of all Maps

RCV (IRV) or Cumulative Voting

Voting as a Mean Field Game

Ensemble Generation Algorithms