

$$\Phi_n(z) \equiv 0 \iff z \text{ has order } n \text{ in } S^1$$