

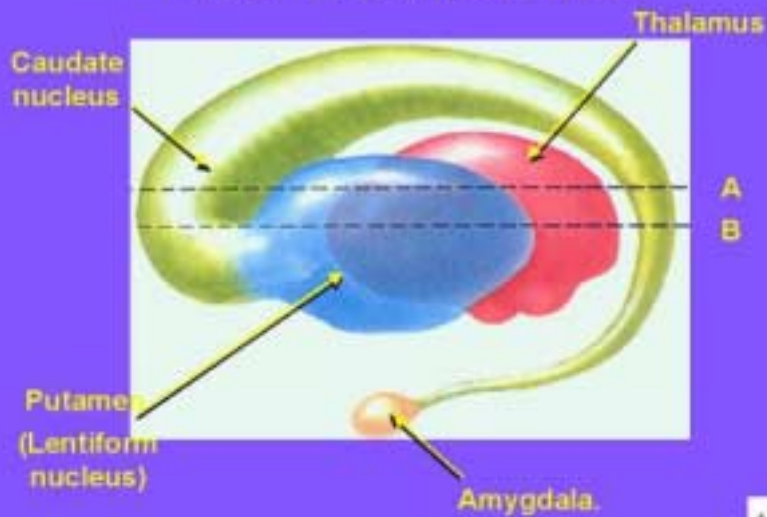
# Firing Patterns in the Subthalamopallidal Network

David Terman  
Ohio State University  
Mathematical Biosciences Institute

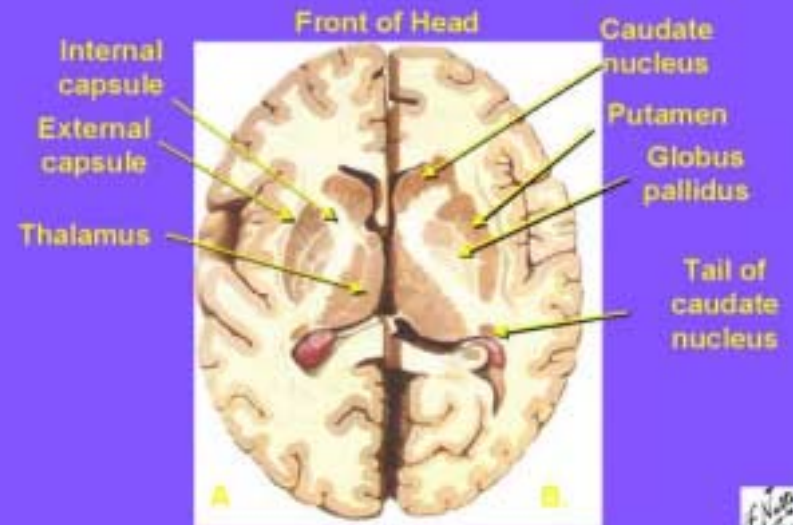
MSRI  
March 17, 2004

# BASAL GANGLIA

## View From Left Side



## Horizontal Section



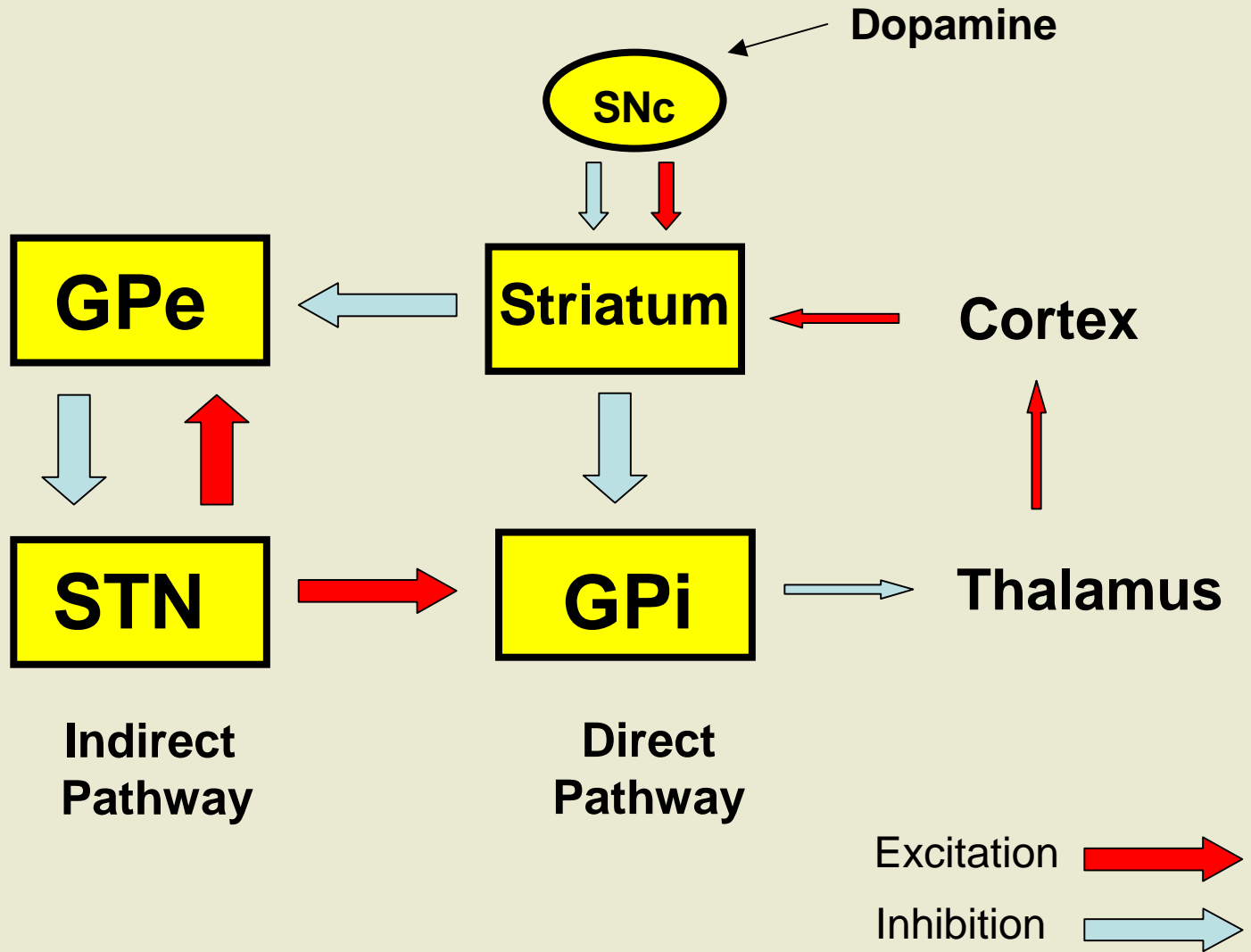
# BASAL GANGLIA

- **Involved in the Control of Movement**
- **Dysfunction Associated with Parkinson's and Huntington's Disease**
- **Site of Surgical Procedures**
  - **Deep Brain Stimulation (DBS)**

# Motivation of Computational Study

- **Previous Models for Neuronal Activity in BG are Static, Based on Mean Firing Rate.**
- **Recent Experiments have Shown that Pattern of Neuronal Activity may be Important.**
- **During PD, Neurons Display:**
  - Increased Synchrony
  - Increased Bursting Activity
- **Earlier Models do not Explain Tremor.**
- **Mechanism Underlying DBS Mysterious.**

# BASAL GANGLIA



Note: Other Pathways May Be Important

# Parkinson's Disease

- ***Movement Disorder***
  - **Slowness of Movement**
  - **Inability to Initiate Movement**
  - **Rigidity**
  - **Tremor**
- ***Reduction of Dopamine***
- ***Increased Activity in Output Nuclei***

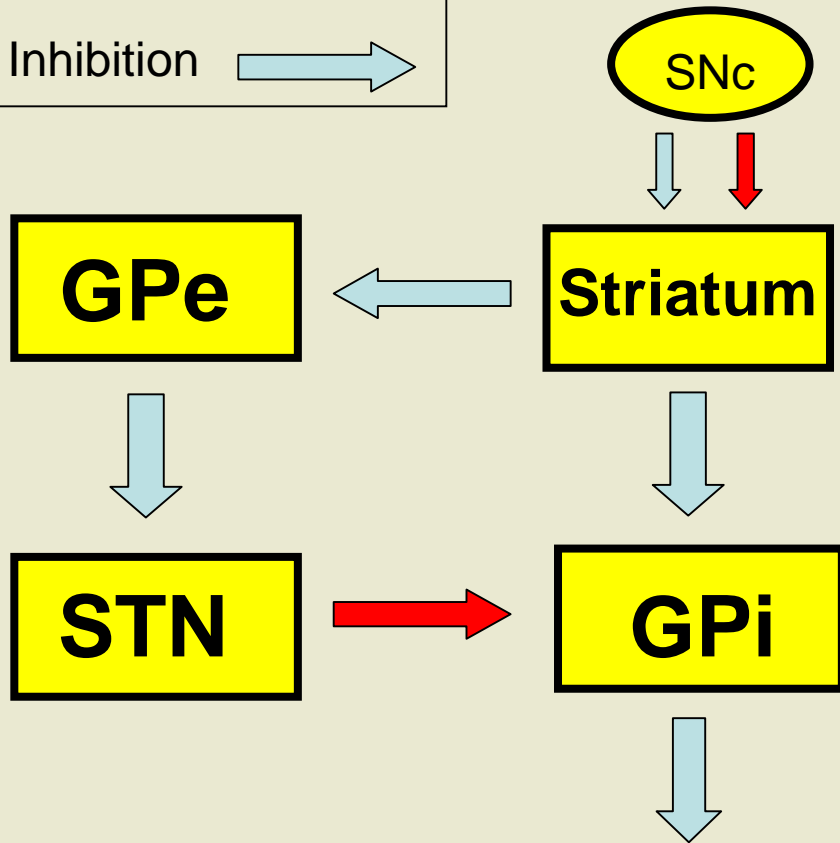
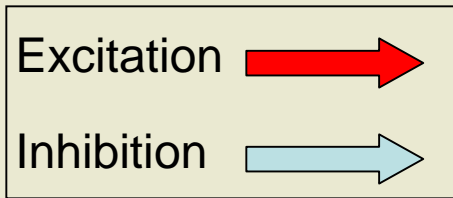
# Parkinson's Disease

- *Movement Disorder*
  - Slowness of Movement
  - Inability to Initiate Movement
  - Rigidity
  - Tremor
- *Reduction of Dopamine*
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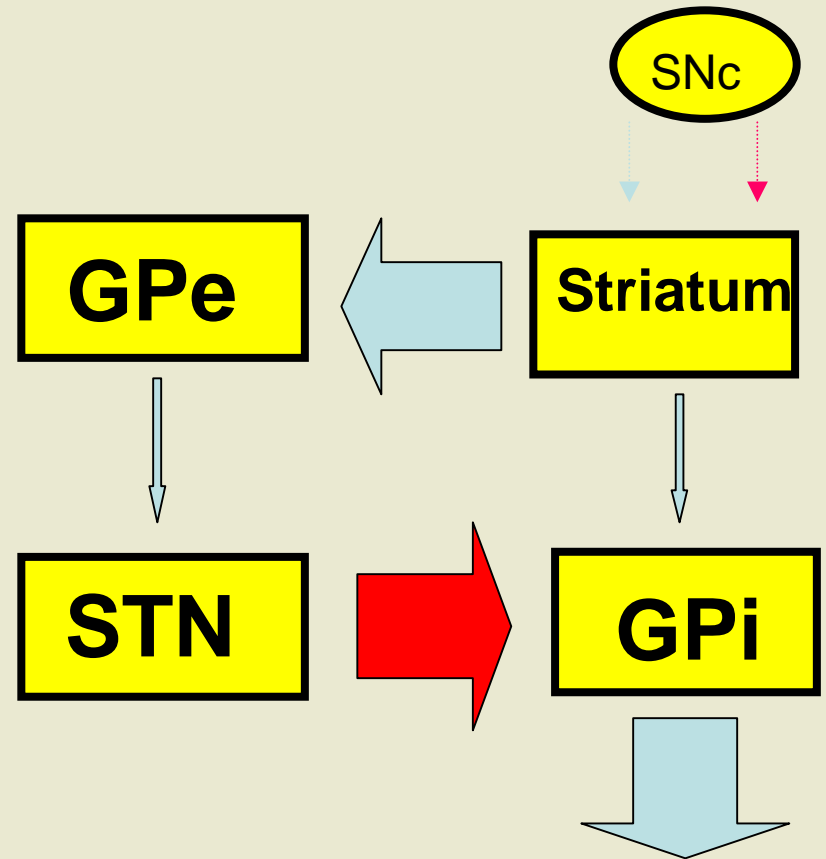
**QUESTION: How Does the Loss of Dopamine Lead to Increased Activity in Output Nuclei?**

# Standard Theory

(Albin / DeLong)



**Normal**



**Parkinsonian**

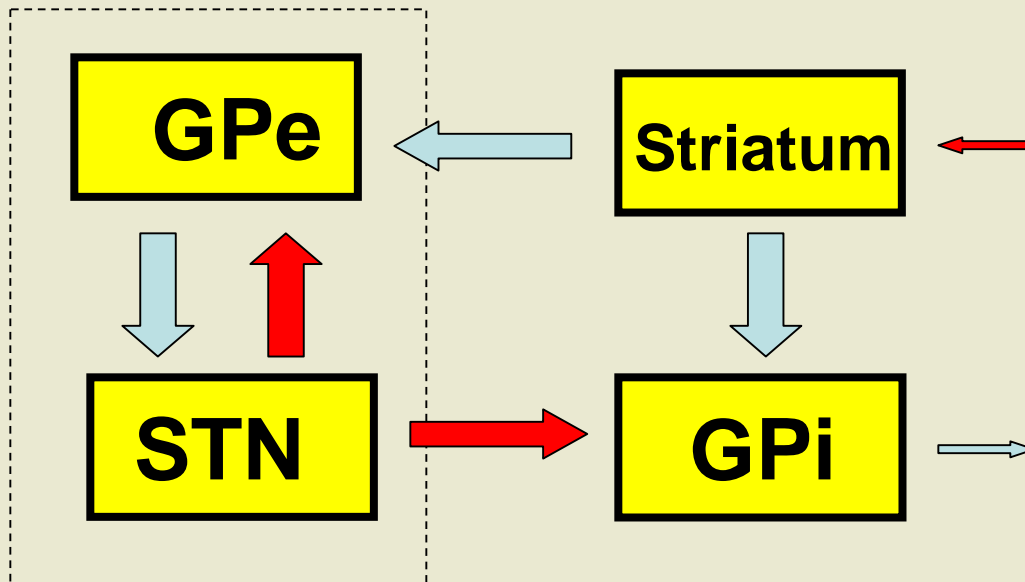


- ***Problems With The Standard Theory***
  - **Does Not Explain Tremor**
  - **Unclear if GPe Activity Decreases in Parkinsonian State**
  - **Lesions alleviate hyperkinetic disturbances**

- ***Problems With The Standard Theory***
  - Does Not Explain Tremor
  - Unclear if GPe Activity Decreases in Parkinsonian State
  - Lesions alleviate hyperkinetic disturbances
  
- ***Possible Explanations***
  - Only Considers Mean Firing Rate
  - Role of Inhibition/Excitation More Complicated
  - Pattern of Activity May Be Important
  - Synchronization

# Experimental Results

- **Neurons Display Increased Synchrony During Parkinsonian State**
- **Isolated GPe/STN Network Can Generate Synchronous Rhythms** (Plenz, Kitae – slow rhythm)



# **MODELING STUDY**

(T., Rubin, Yew, Wilson)

- **Construct Model GPe/STN Network.**
- **Can Such a Network Generate Synchronous, Tremor-Like Rhythms?**
- **What Other Activity Patterns Arise?**
- **Reinterpret Role of Indirect Pathway.**

# MODEL STN NEURON

$$C_M \frac{dV}{dt} = -I_L - I_K - I_{Na} - I_T - I_{AHP} - I_{Ca}$$

$$\begin{aligned} I_L &= g_L(V - V_L), & I_K &= g_K n^4 (V - V_K), \\ I_{Na} &= g_{Na} m^3(V) (V - V_{Na}), & I_T &= g_T a_\infty^3(V) b_\infty^2(r) (V - V_{Ca}), \\ I_{Ca} &= g_{Ca} s_\infty^2(V) (V - V_{Ca}), & I_{AHP} &= g_{AHP} \frac{[Ca]}{[Ca] + k} (V - V_K) \end{aligned}$$

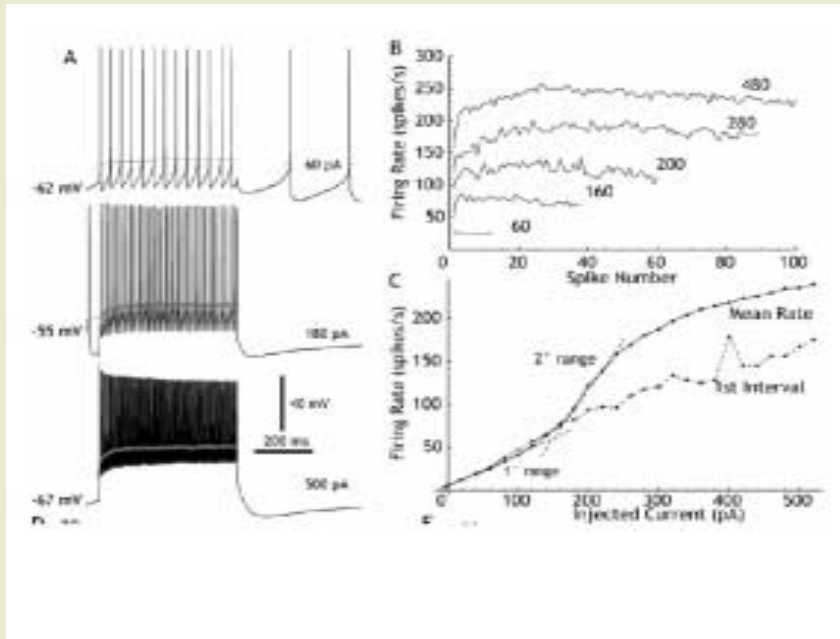
$$X' = \phi_X \left( \frac{X_\infty(V) - X}{\tau_X(V)} \right), \quad X = n, h, r$$

$$[Ca]' = \epsilon(-I_{Ca} - I_T - k_{Ca}[Ca])$$

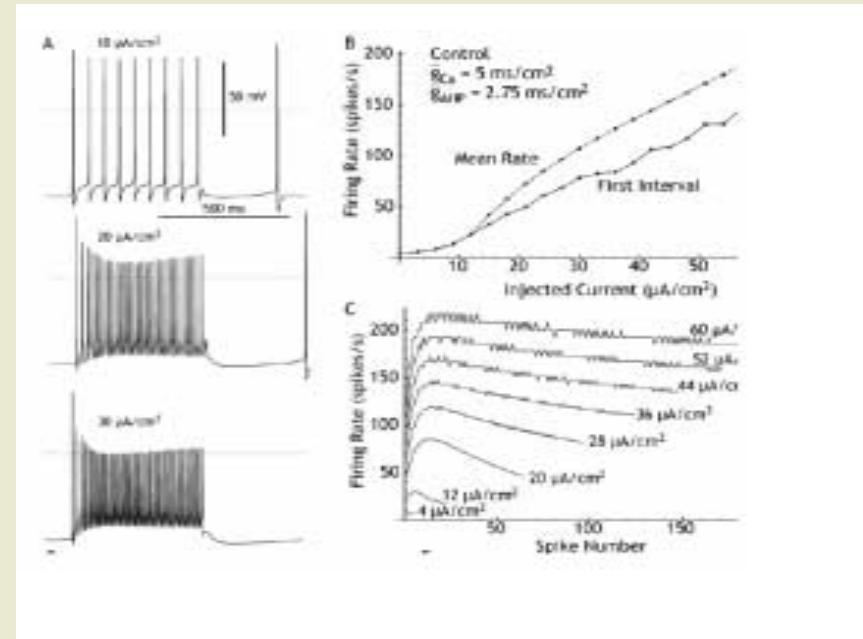
Based on Experiments  
(Bevan and Wilson)

# Firing Properties of STN Cells

## Experiment

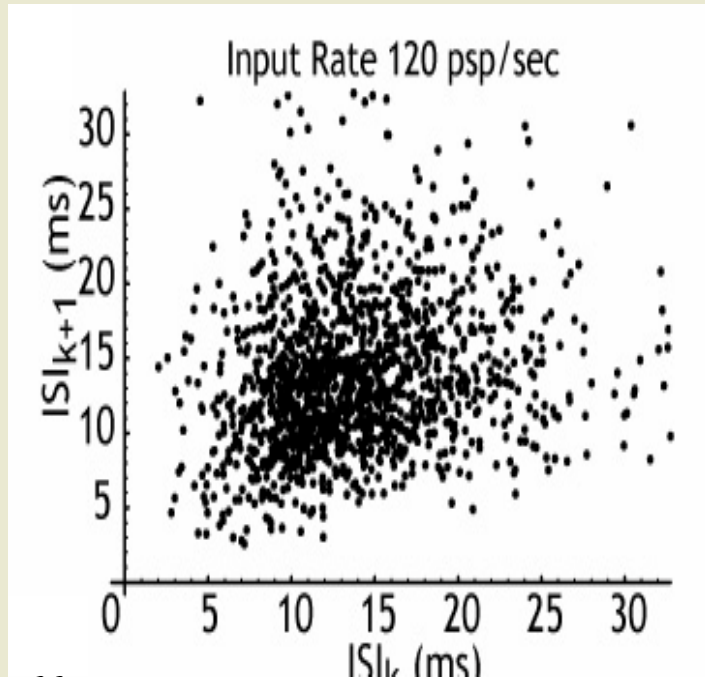


## Model

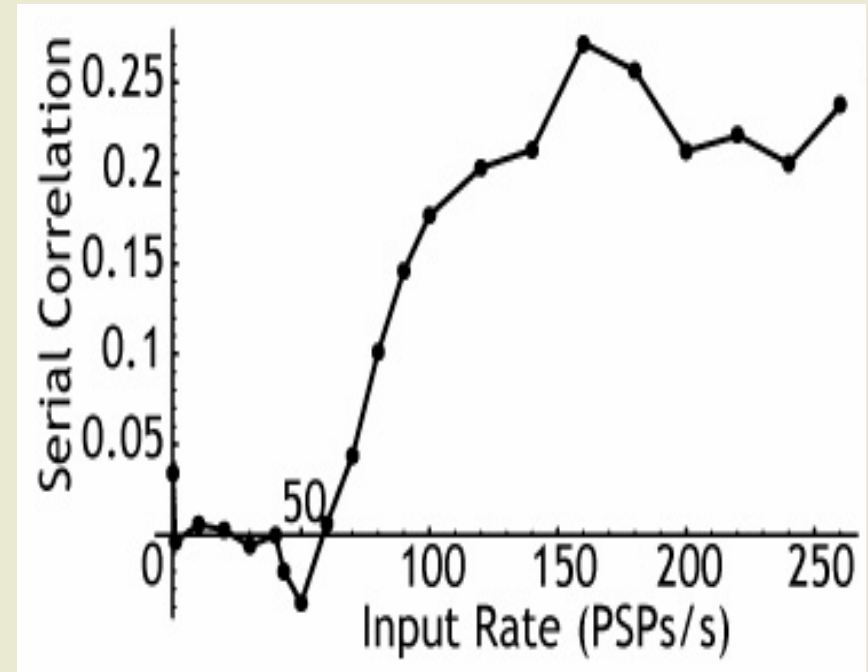


- High Frequency Firing with Applied Current
- Secondary Range in F-I Curve
- Reverse Spike Frequency Adaptation

# Reverse Spike Frequency Adaptation Leads to Increased Correlation of Incoming Signal



**First Return Map for ISIs**

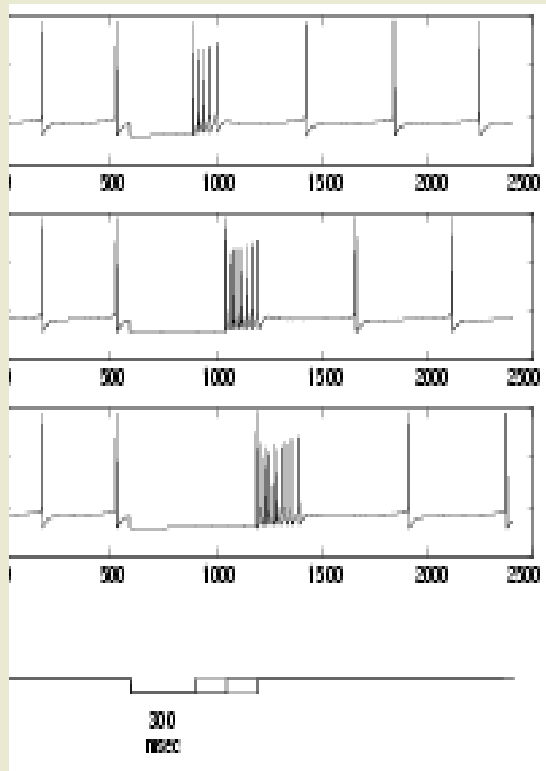


**Serial Correlation**

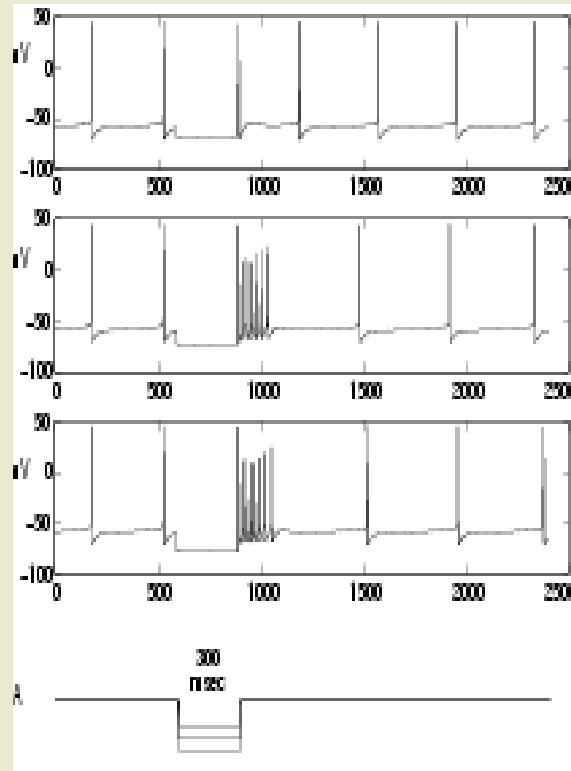
(Wilson, Weyrick, T., Hallworth, Bevan)

# Firing Properties of STN/GPE Neurons

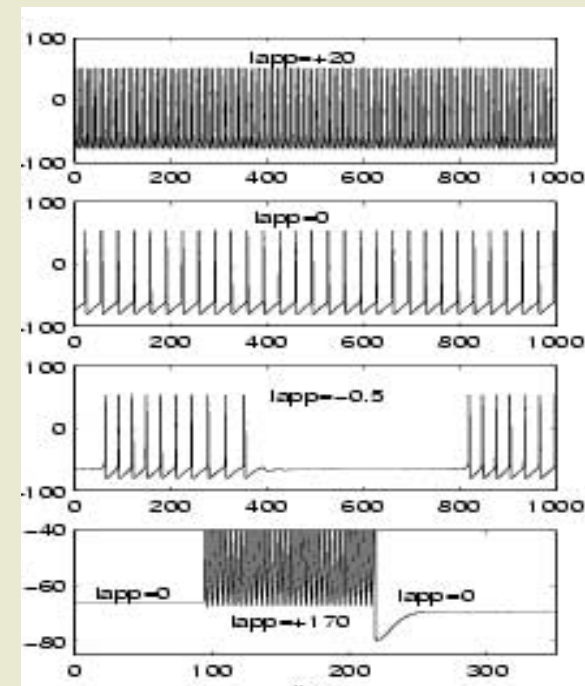
STN



Post Inhibitory Rebound



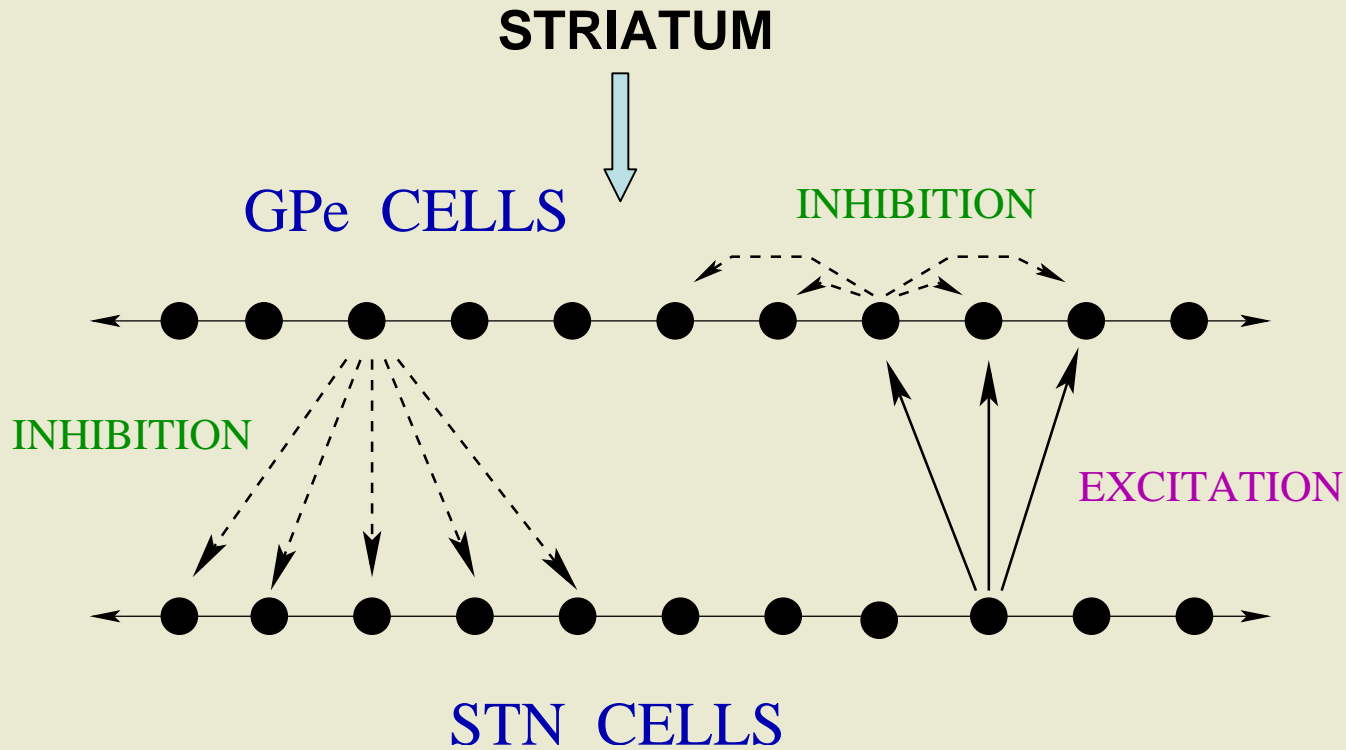
GPE



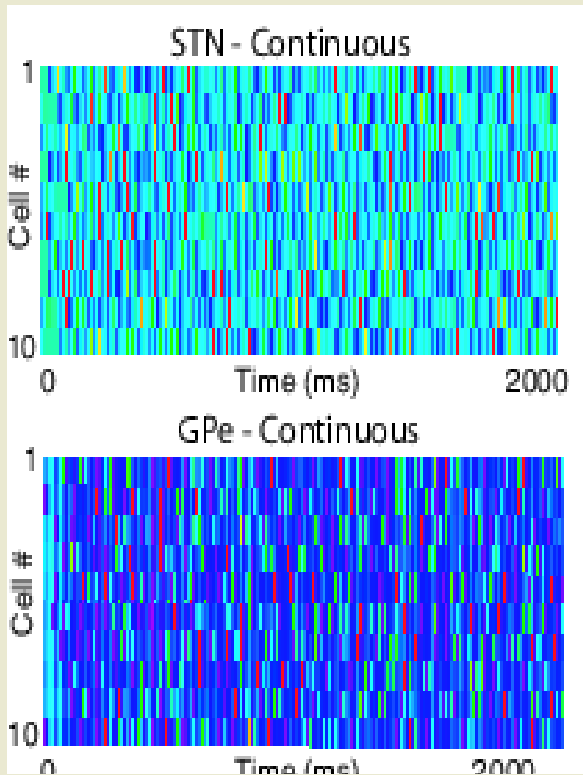
Firing Profiles



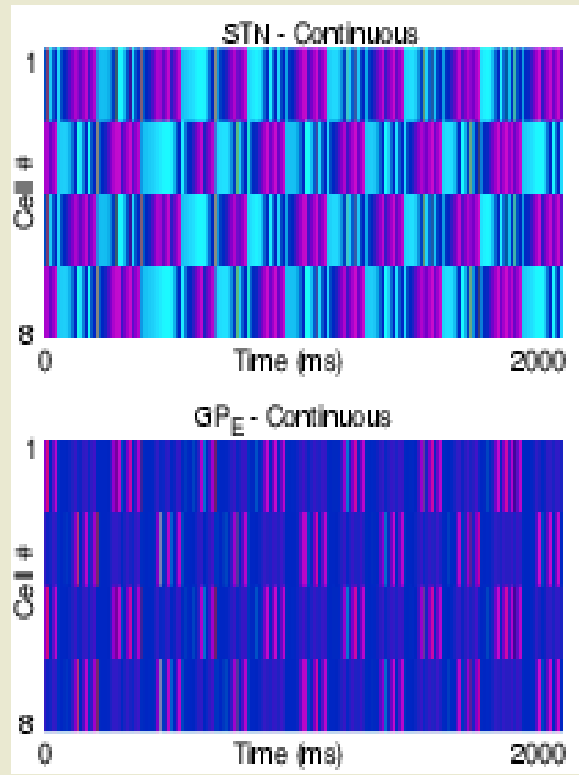
# STN / GPe NETWORK



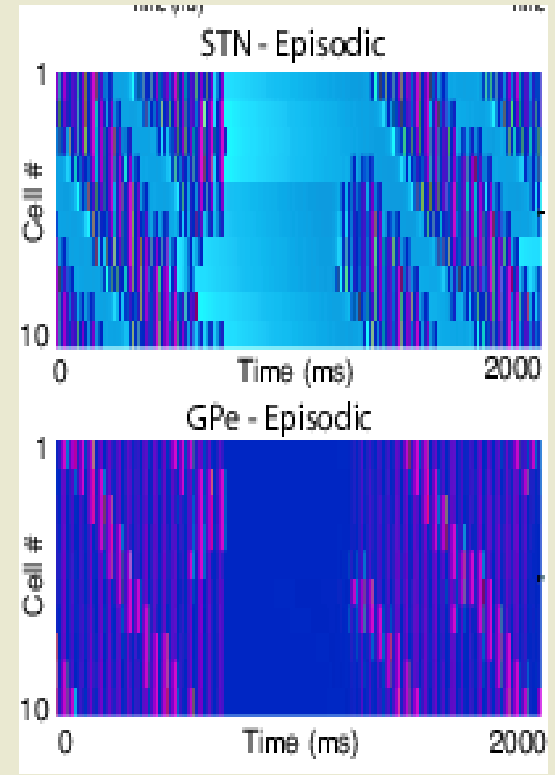
# The Model Exhibits a Variety of Activity Patterns



**Irregular  
(Normal)**

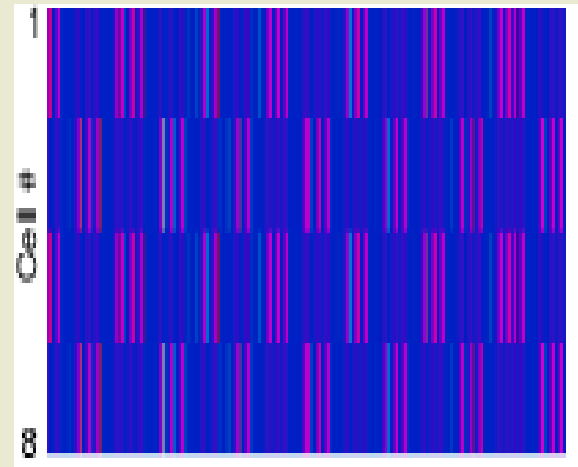
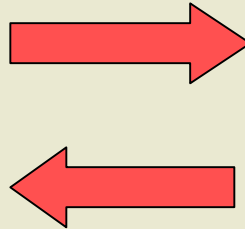
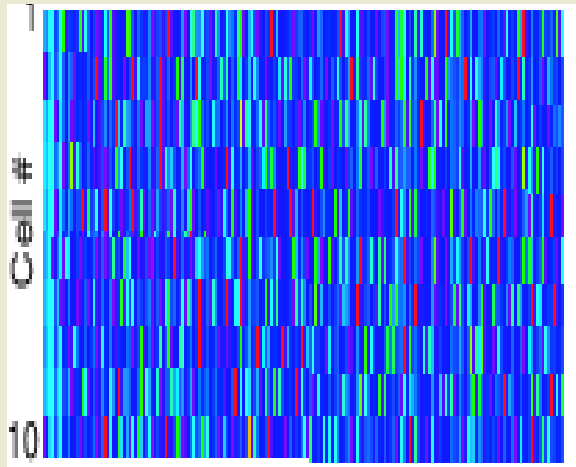


**Synchronous  
Clusters (Park)**



**Propagating  
Waves**

# Transition between Irregular and Rhythmic Activity



**Irregular  
(Normal)**

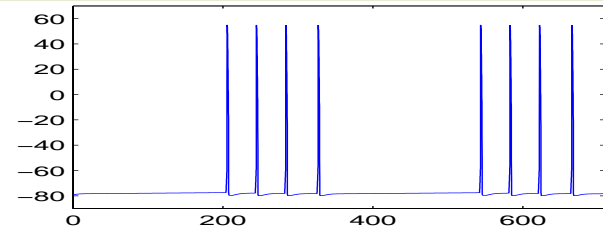
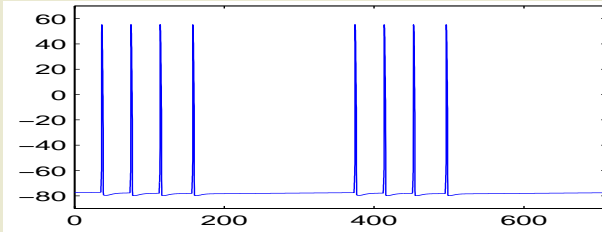
**Clustering  
(Parkinson)**

- **What Parameter Changes Can Account for this Transition ?**
- **Can This Transition Arise Due to Rebound Properties of STN Cells ?**

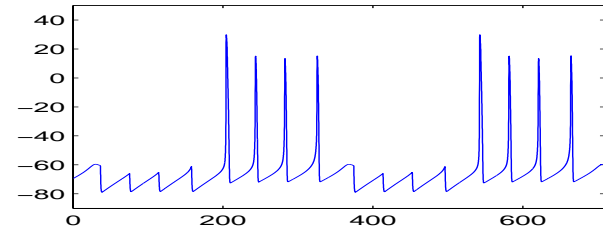
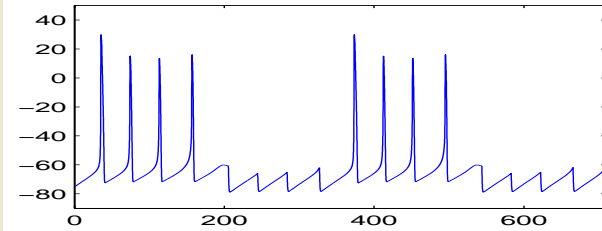
(Best,Park,Wilson,T.)

# Clustering

**GPe**

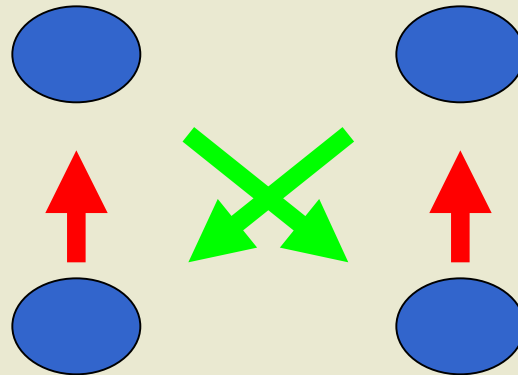


**STN**

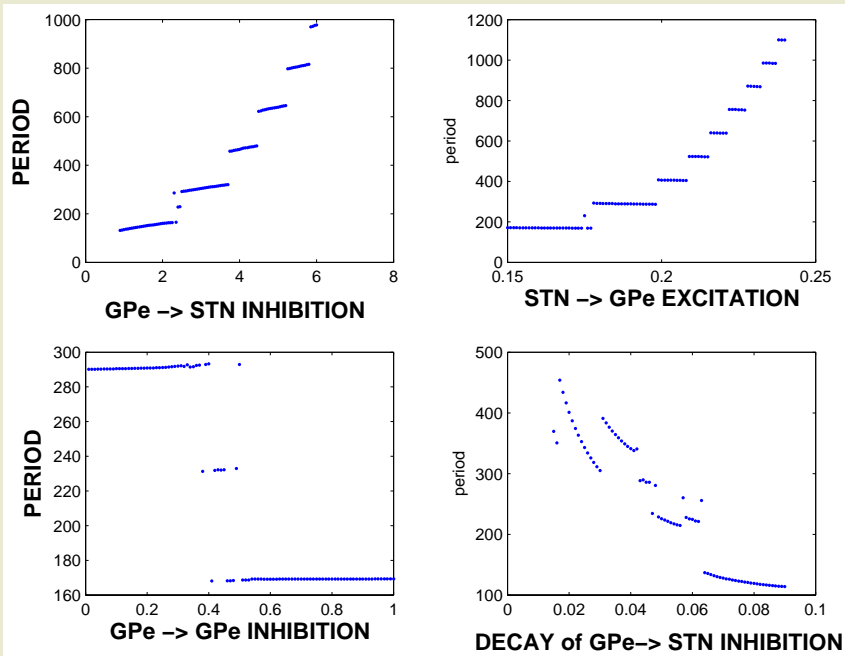


**GPe Cell Fires due to Excitation from STN**

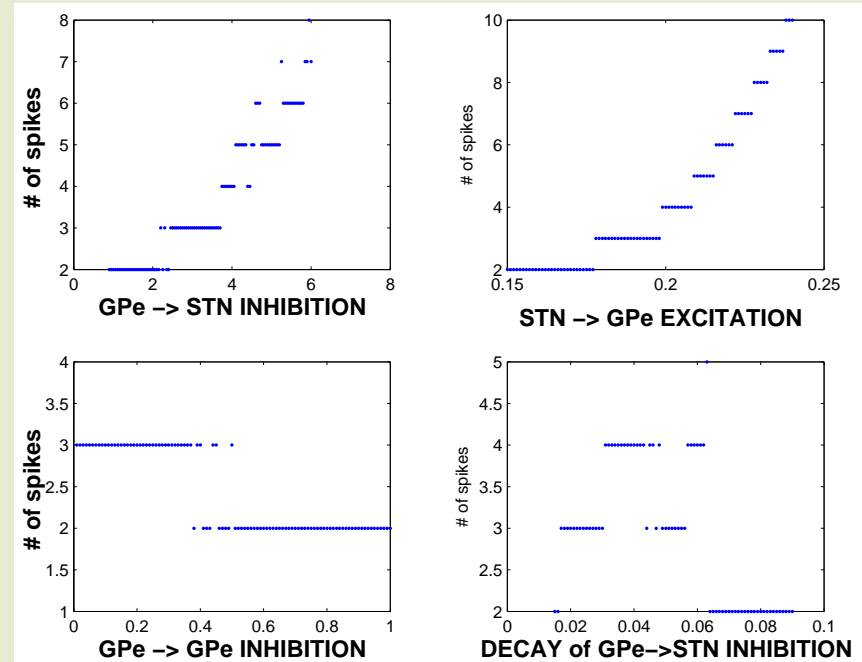
**STN Fires due to Post-Inhibitory Rebound**



# Dependence on Parameters

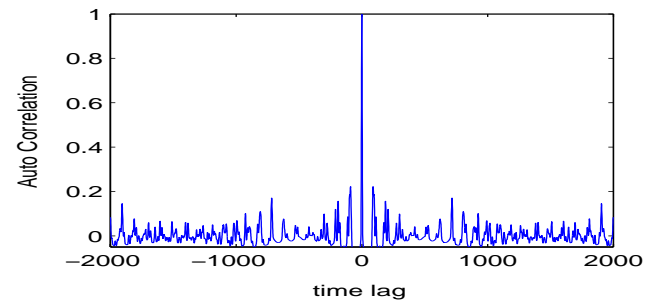
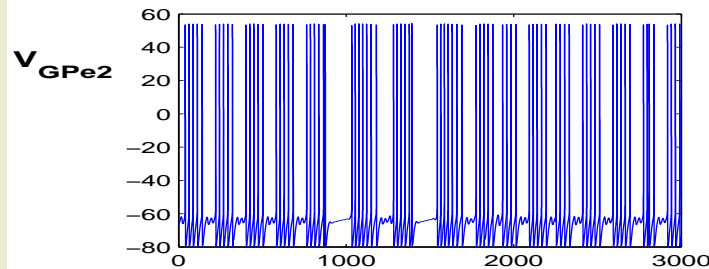
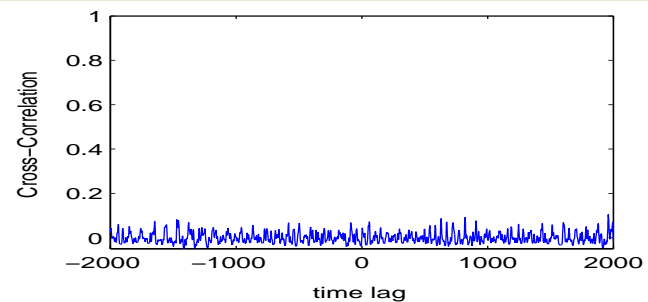
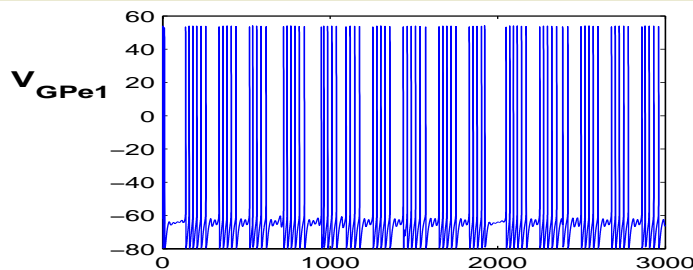
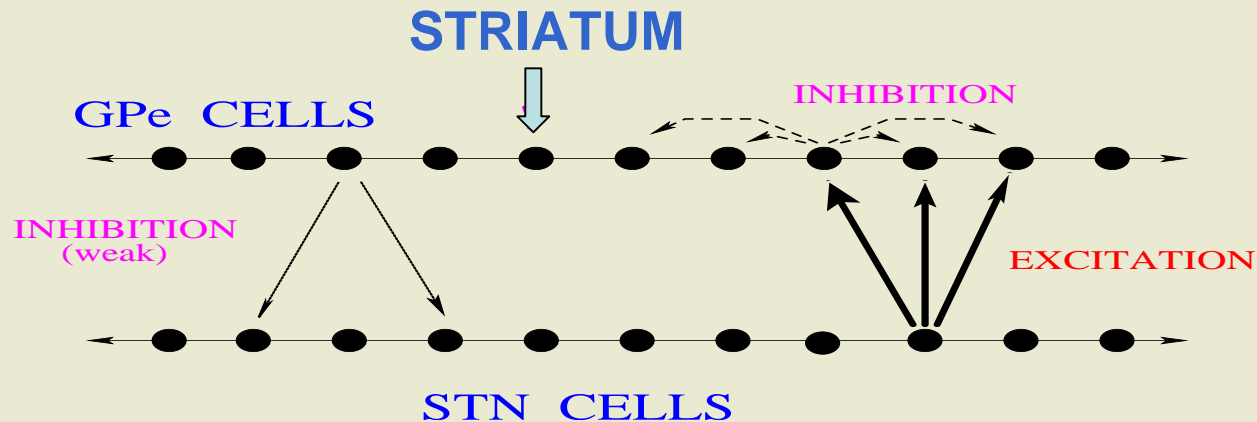


**Period**



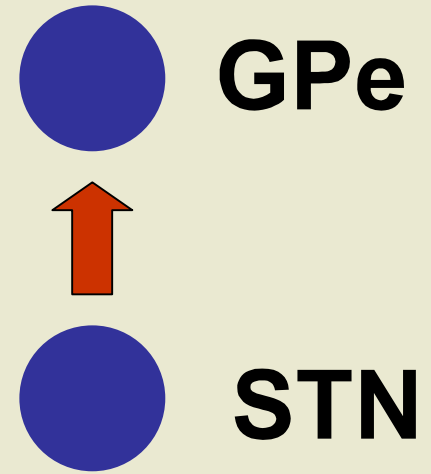
**# Spikes / Cluster**

# Irregular Firing Can Arise if Inhibition to STN Cells is Weak



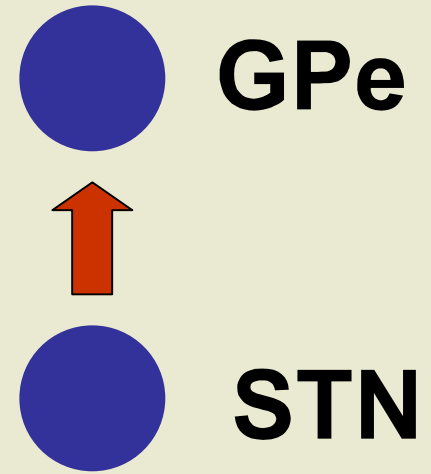
# Analysis of Irregular Firing

**Consider a Periodically  
Forced GPe Cell:**



# Analysis of Irregular Firing

**Consider a Periodically  
Forced GPe Cell:**

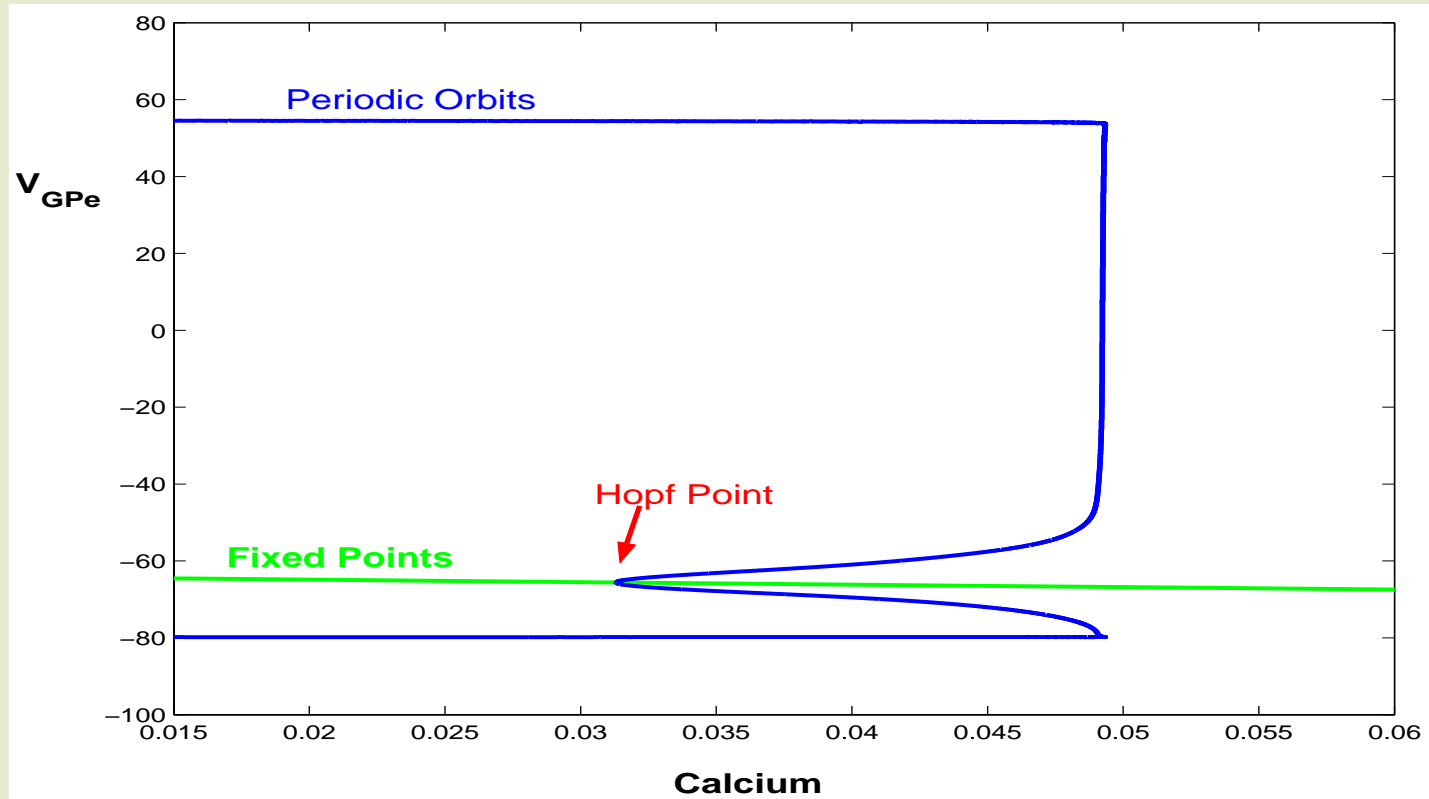


## OUTLINE of ANALYSIS

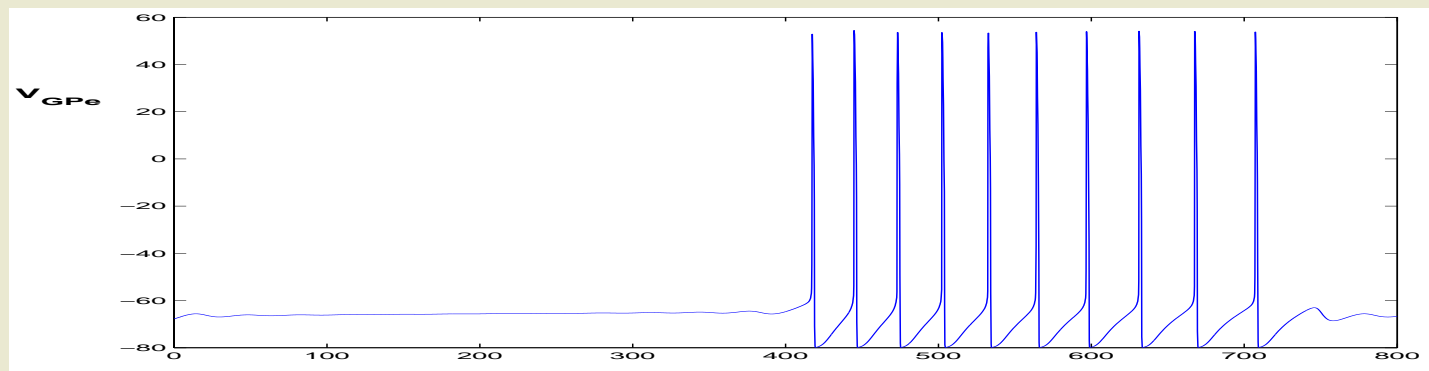
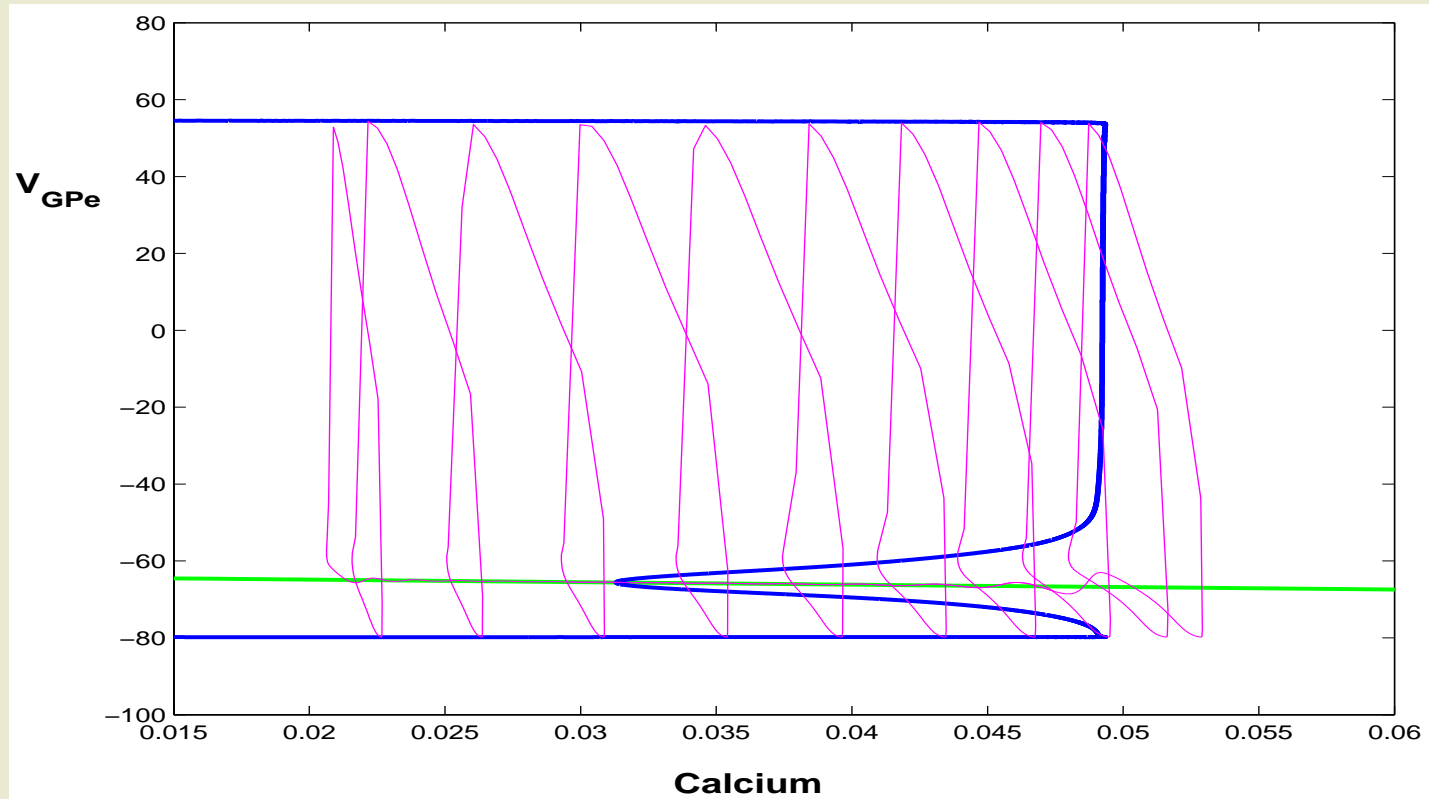
- **Fast/Slow Analysis of GPe Cell**
- **Phase-Response Curve for GPe Cell**
- **Construct a 1-D Map**



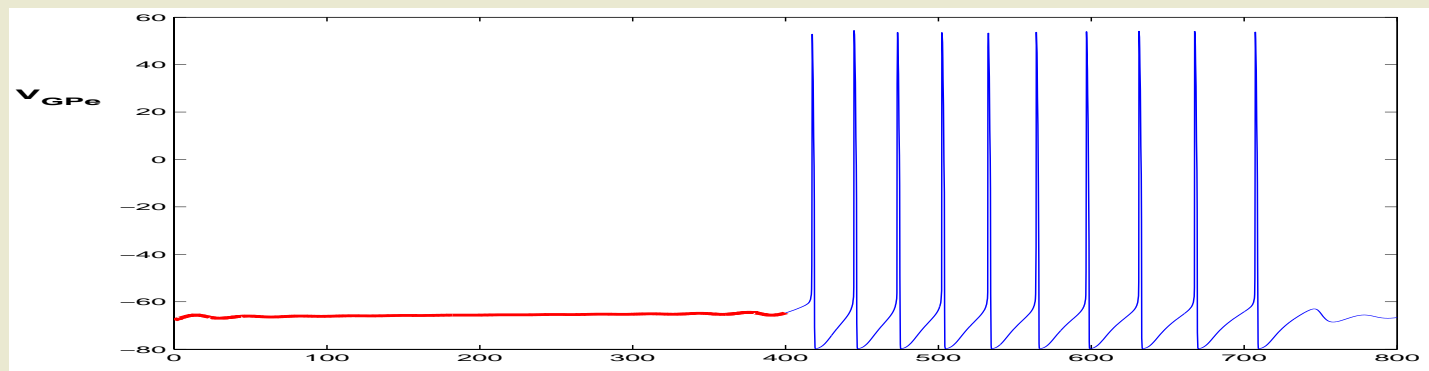
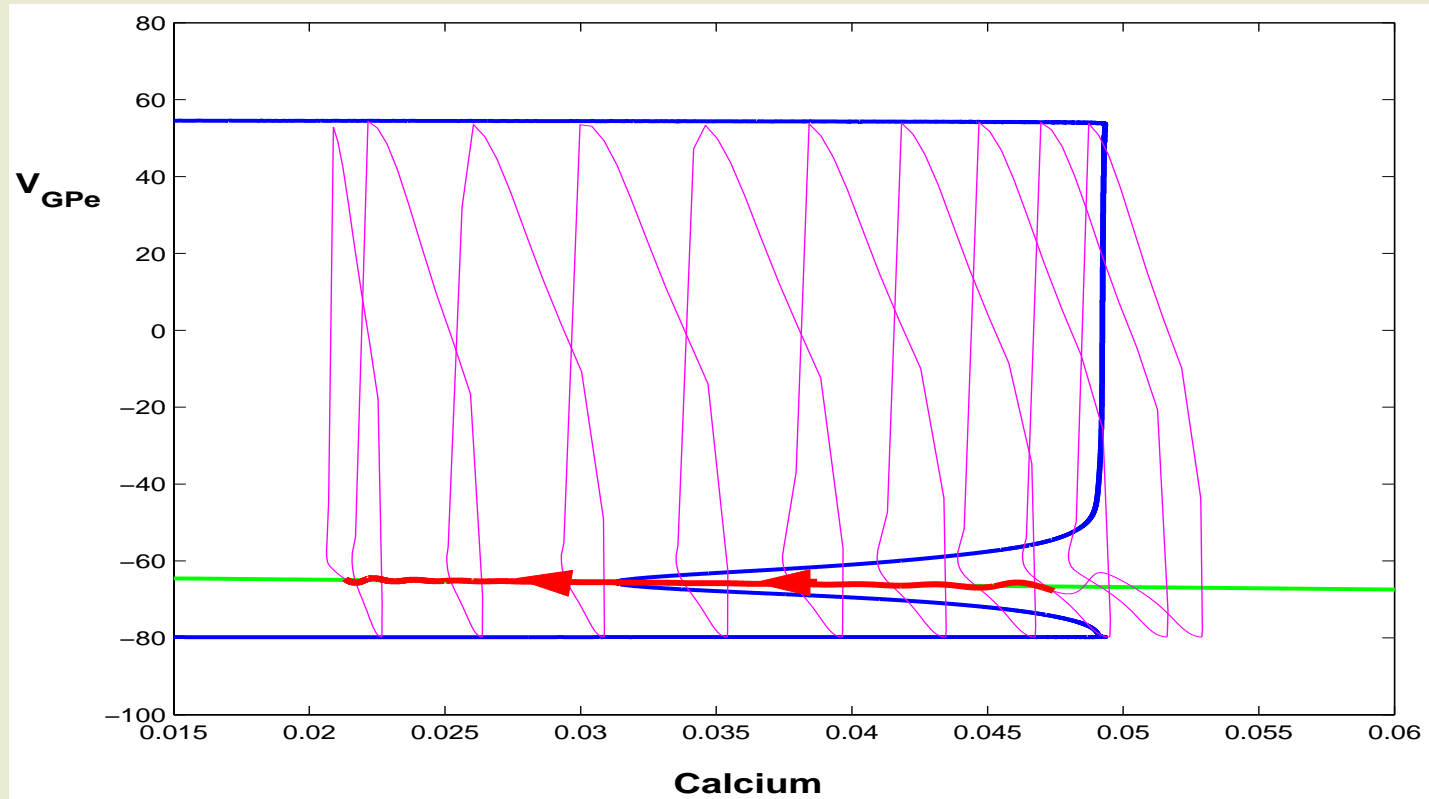
# GPe Cells Are Elliptic Bursters



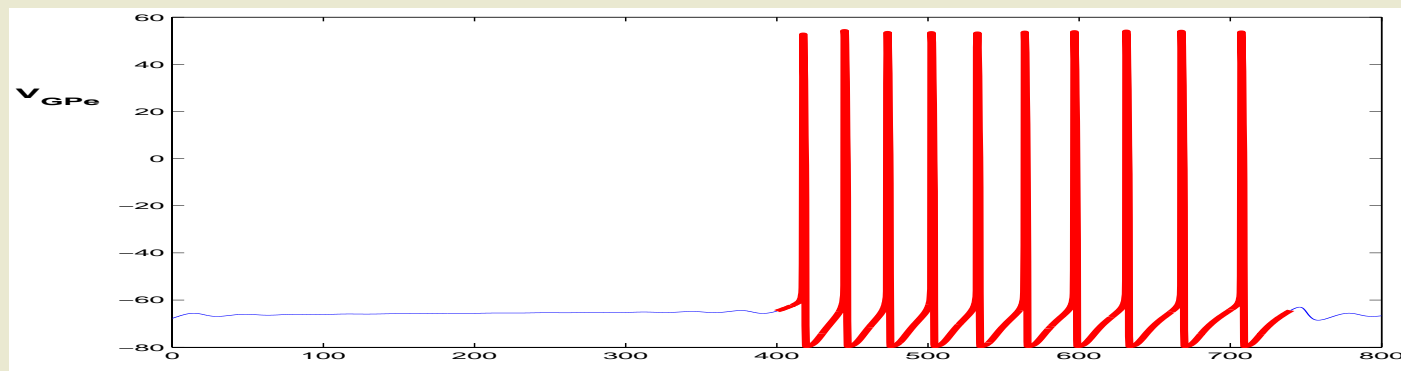
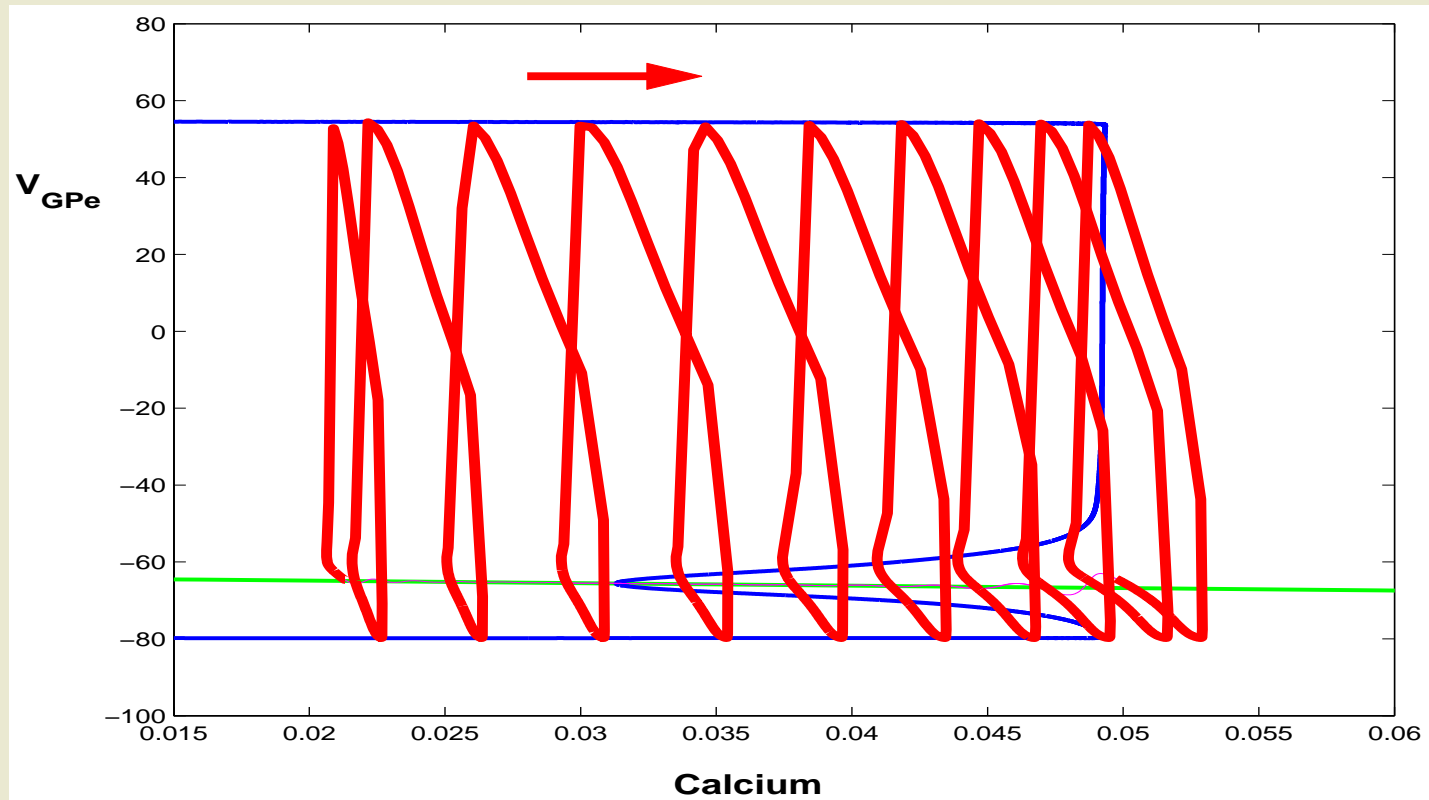
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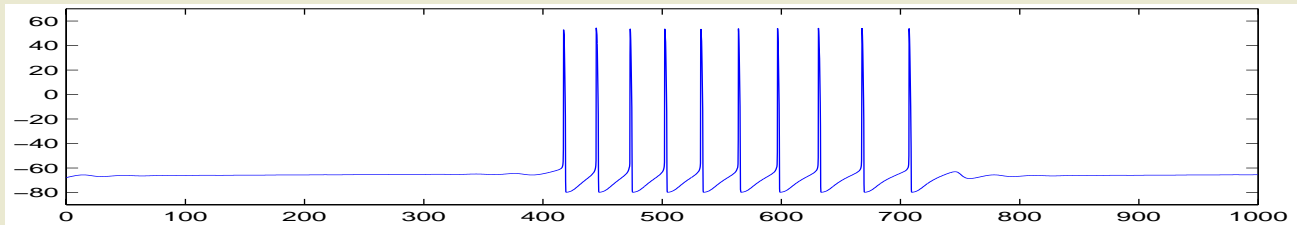


# Dynamics Reduce to a Single Equation for the Slow Variable

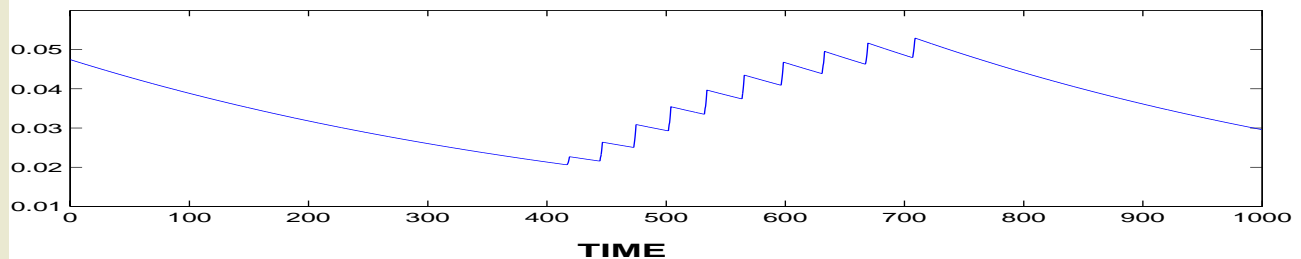
**Good Approximation:**

$$Ca' = \begin{cases} -\lambda_S & \text{cell silent} \\ \lambda_A & \text{cell active} \end{cases}$$

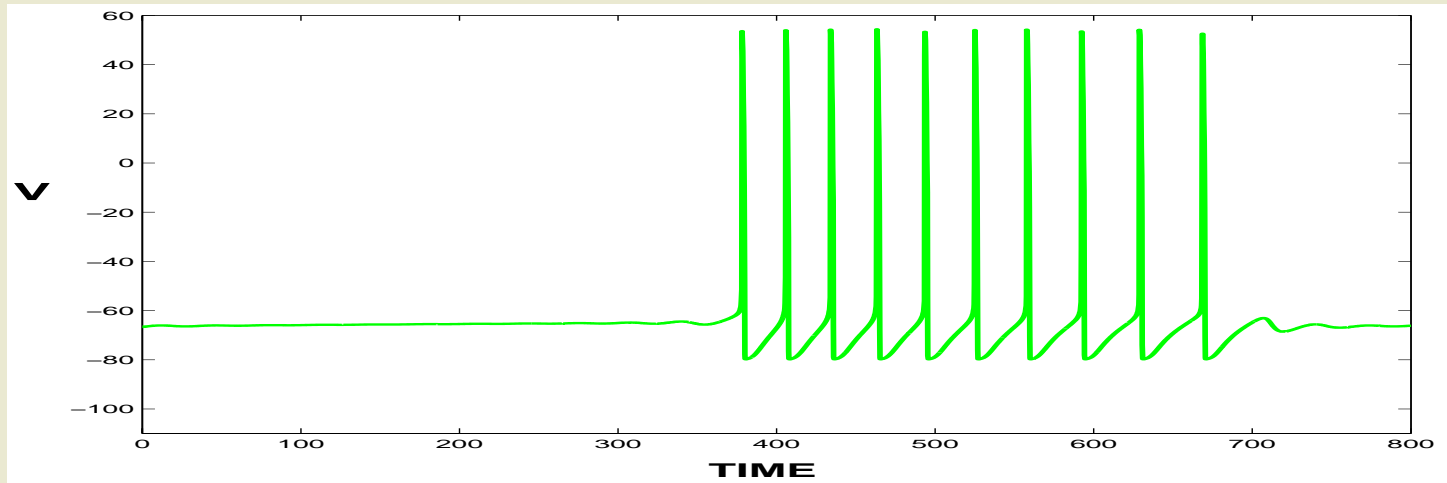
**V<sub>GPe</sub>**



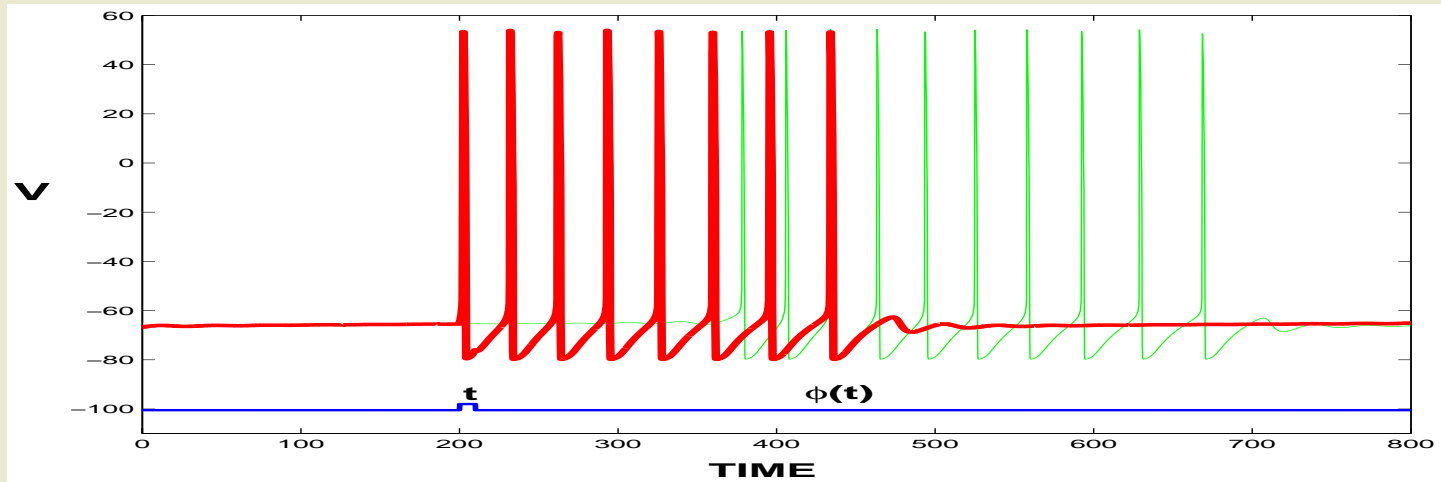
**Ca**



# Phase-Response Curve for GPe Cell



# Phase-Response Curve for GPe Cell

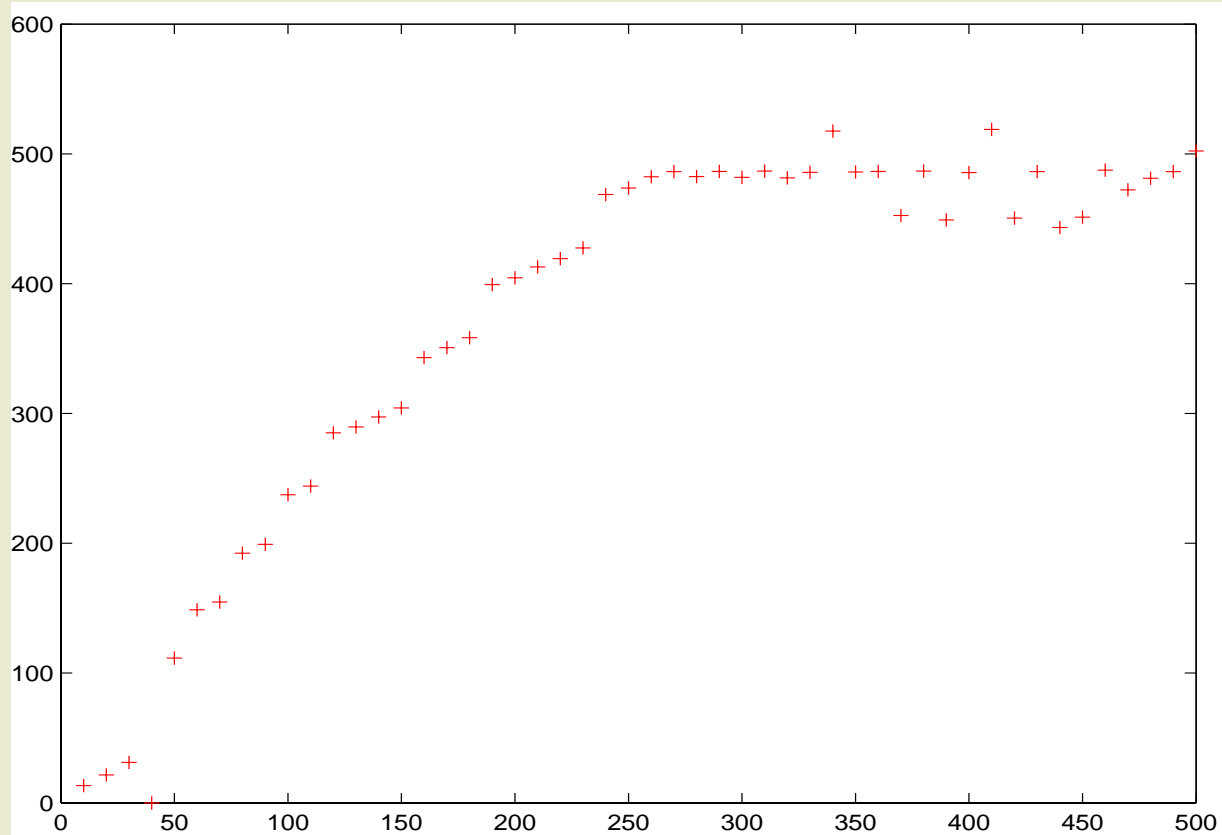


- **Perturb GPe Cell at Time  $t$**
- **$\phi(t)$  = time when GPe cell ends its next active phase**

**Choose  $t=0$  when GPe cell ends an active phase**

# Phase Response Curve

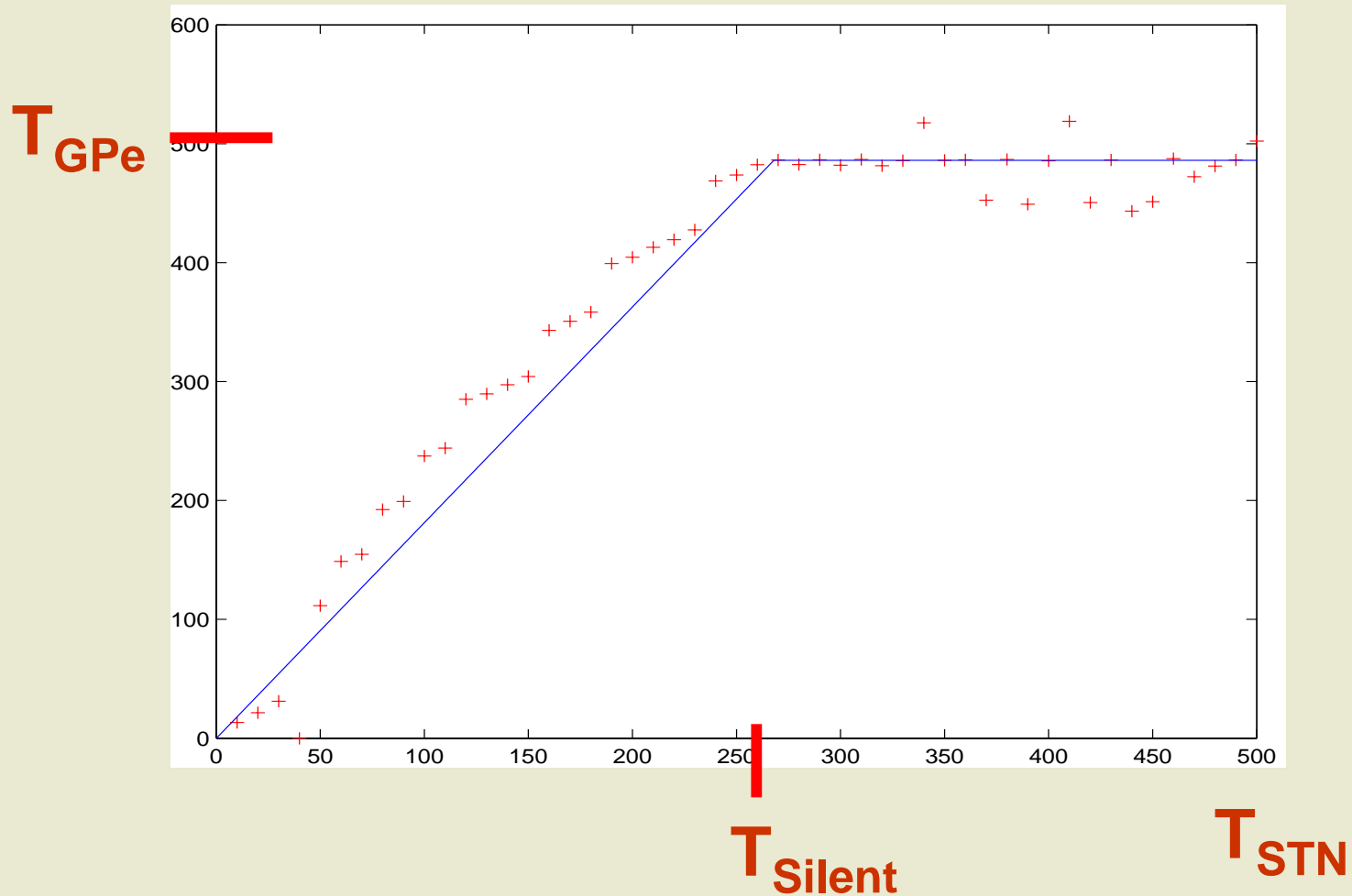
$\phi(t)$



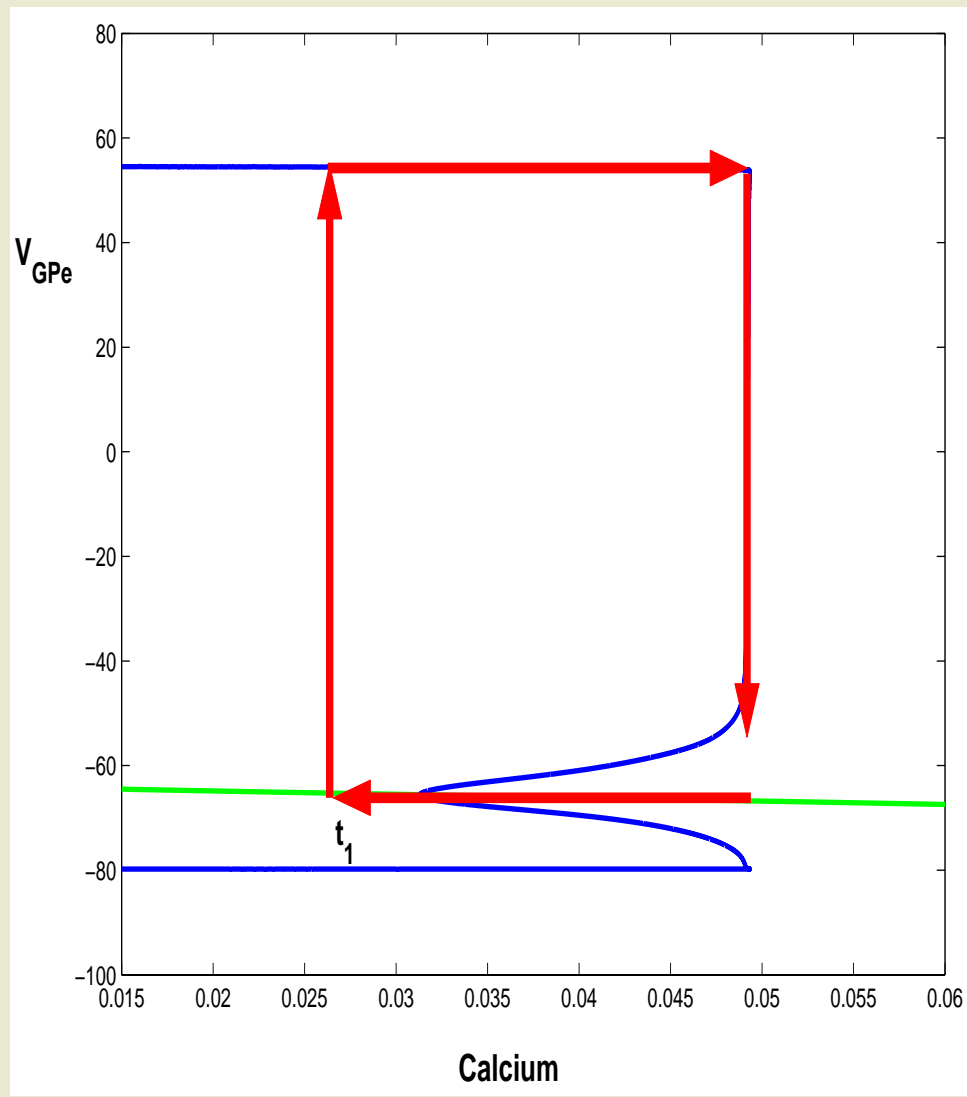
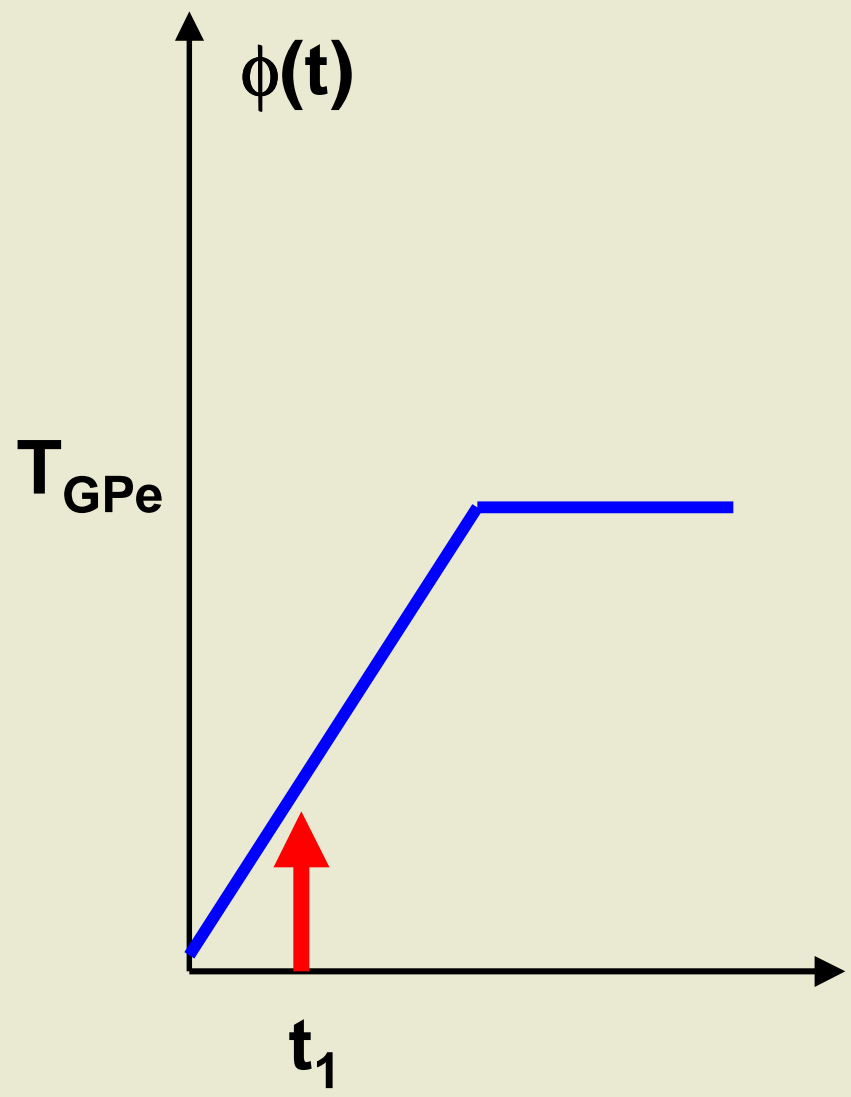
t



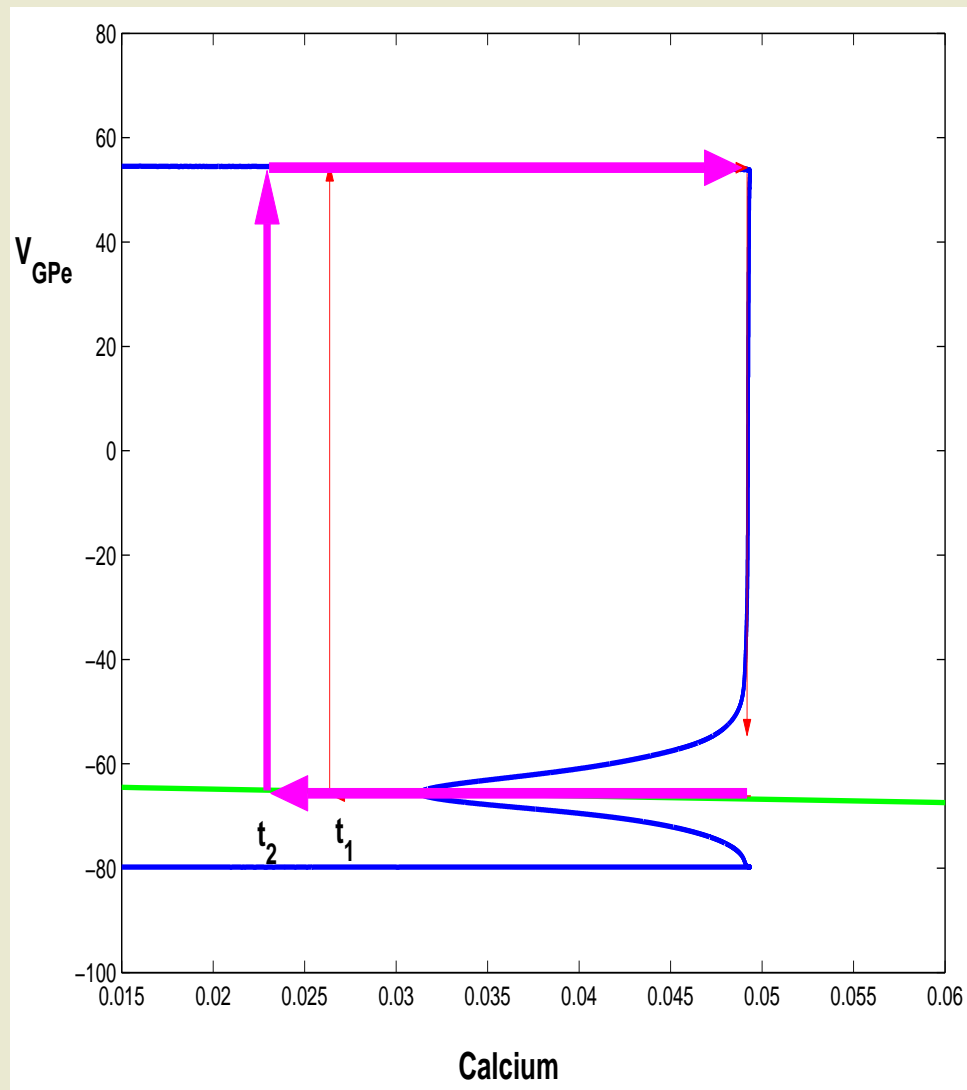
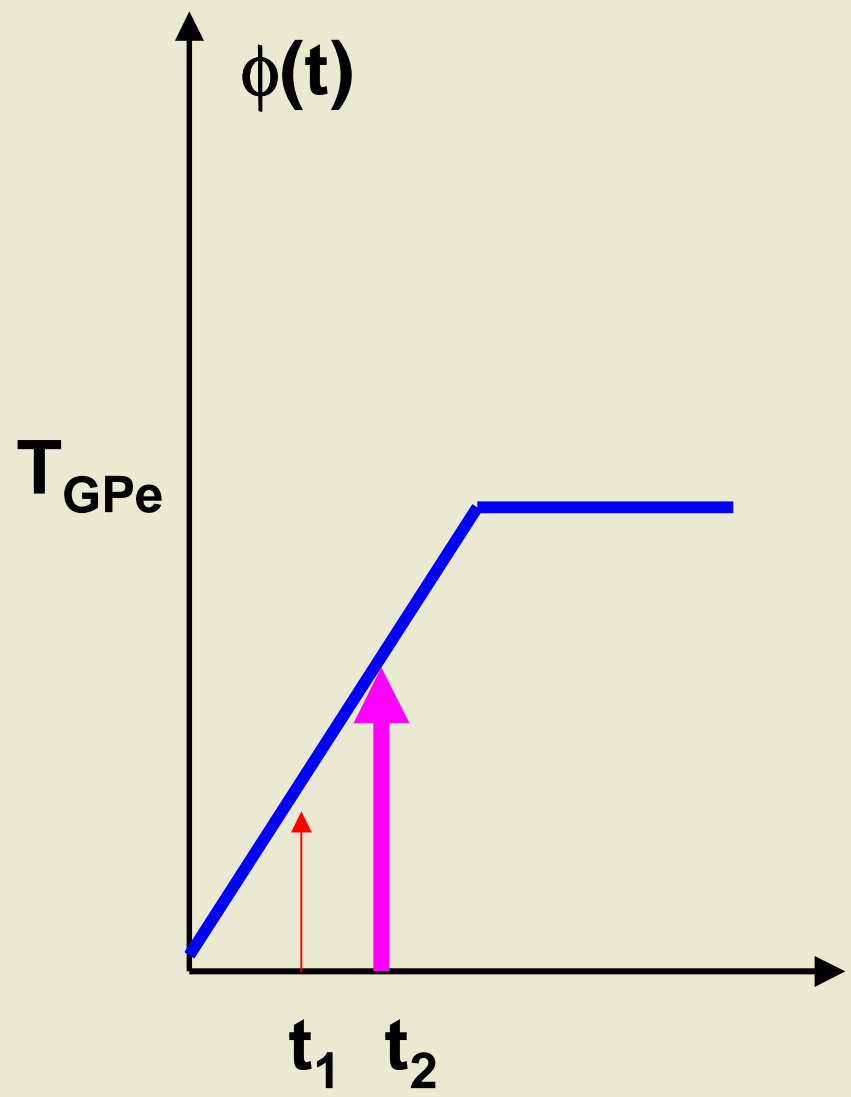
# Phase Response Curve



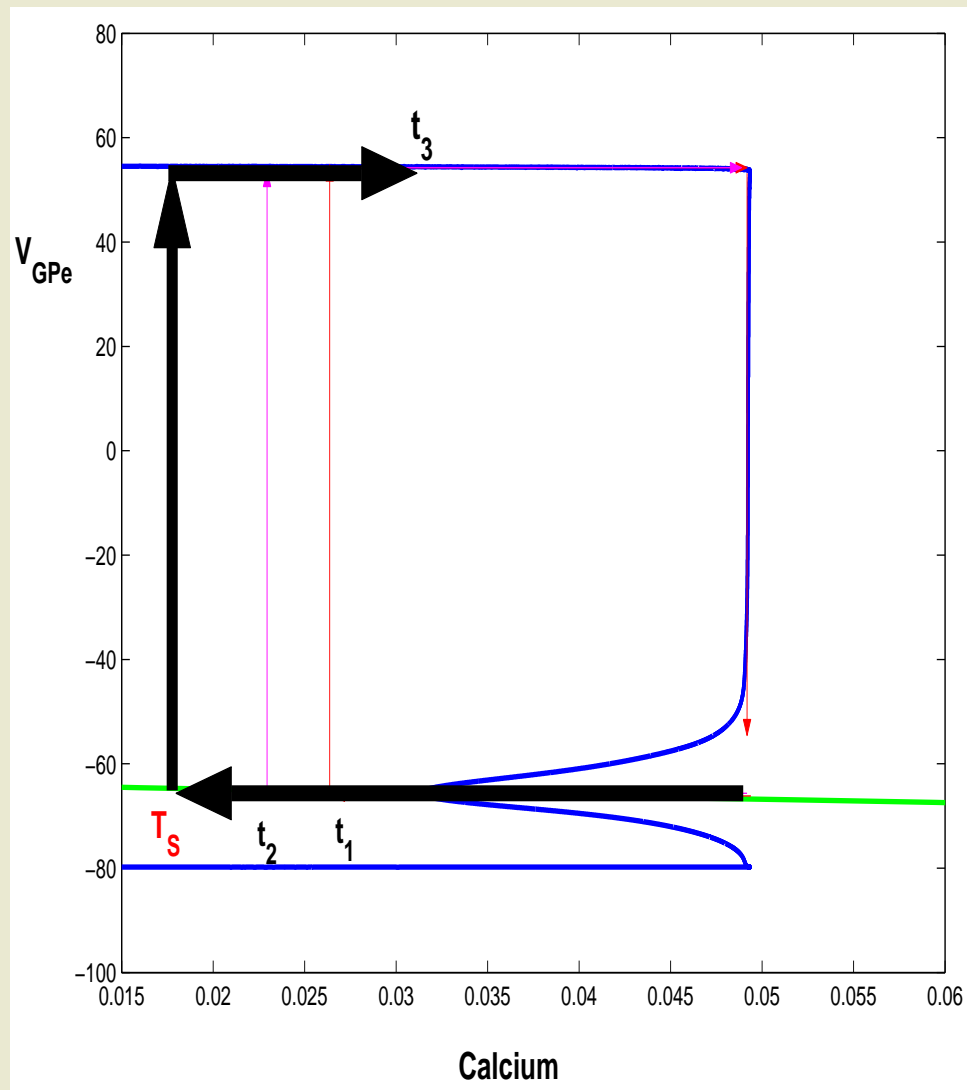
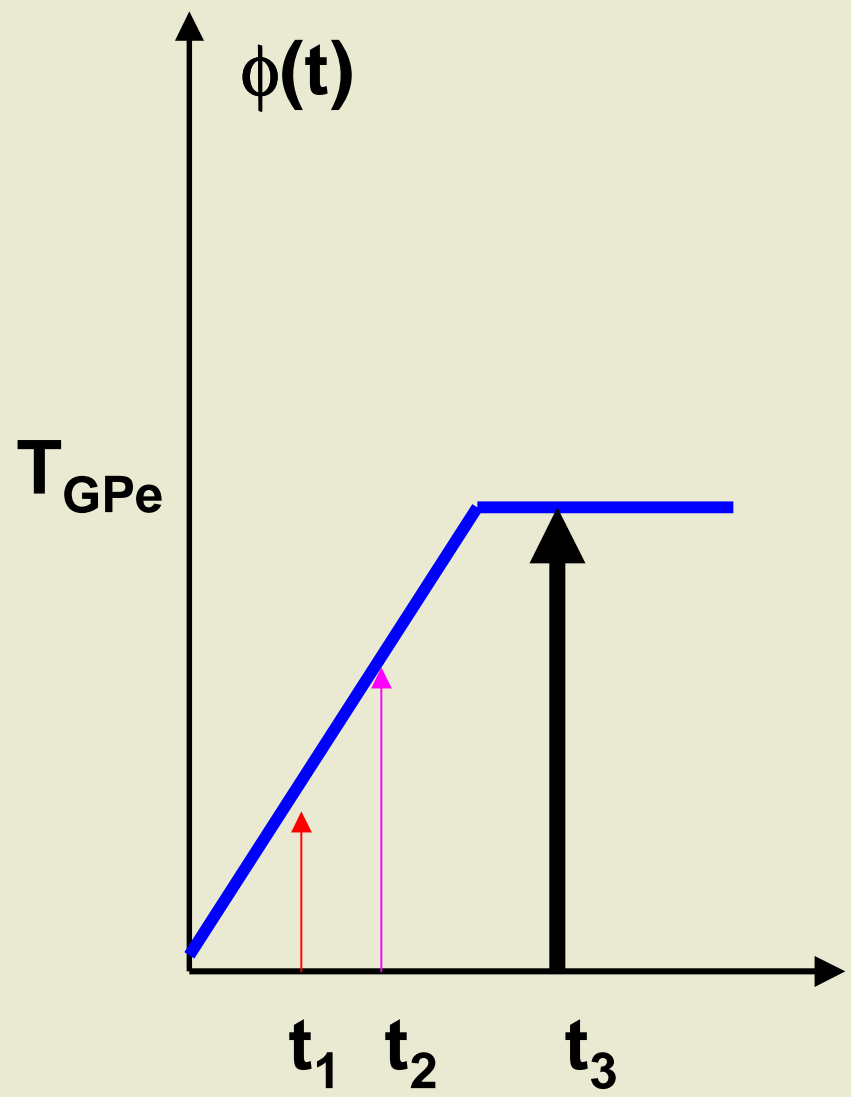
# Phase Response Curve



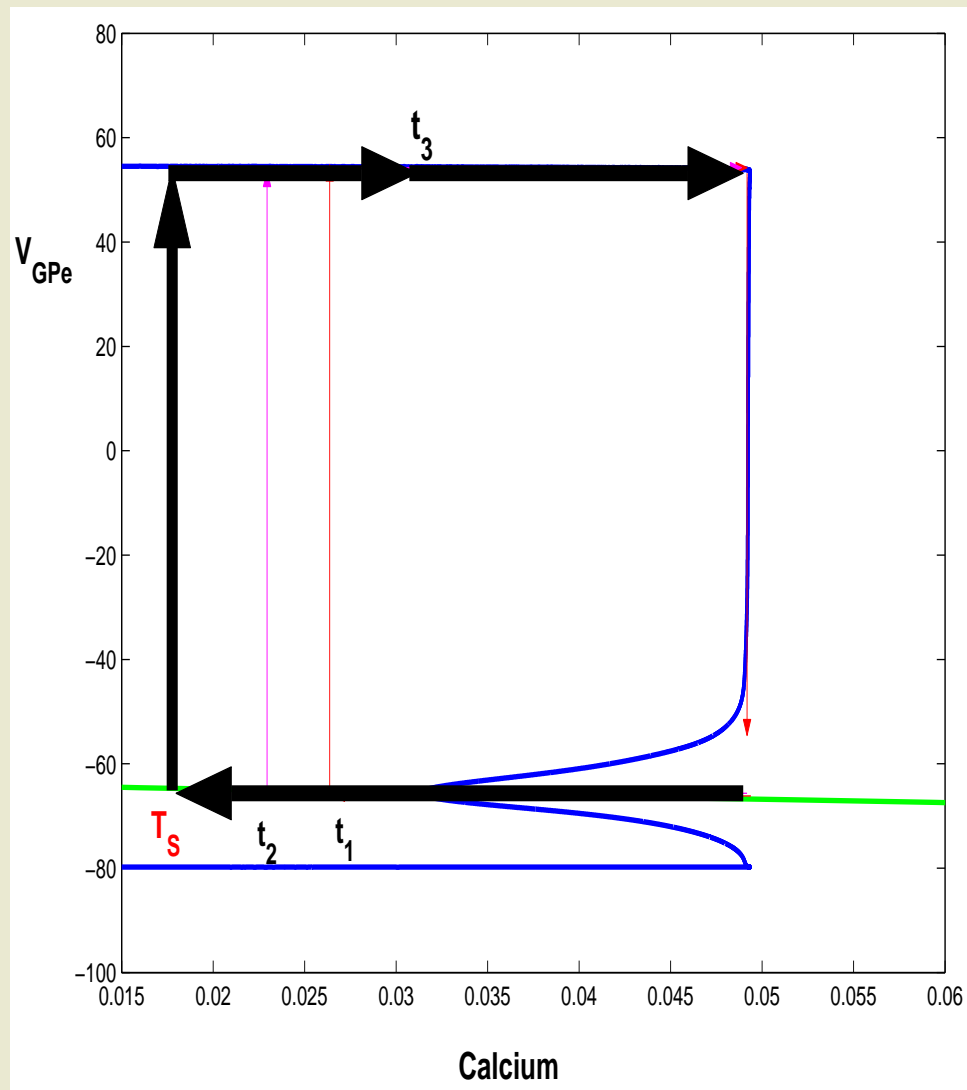
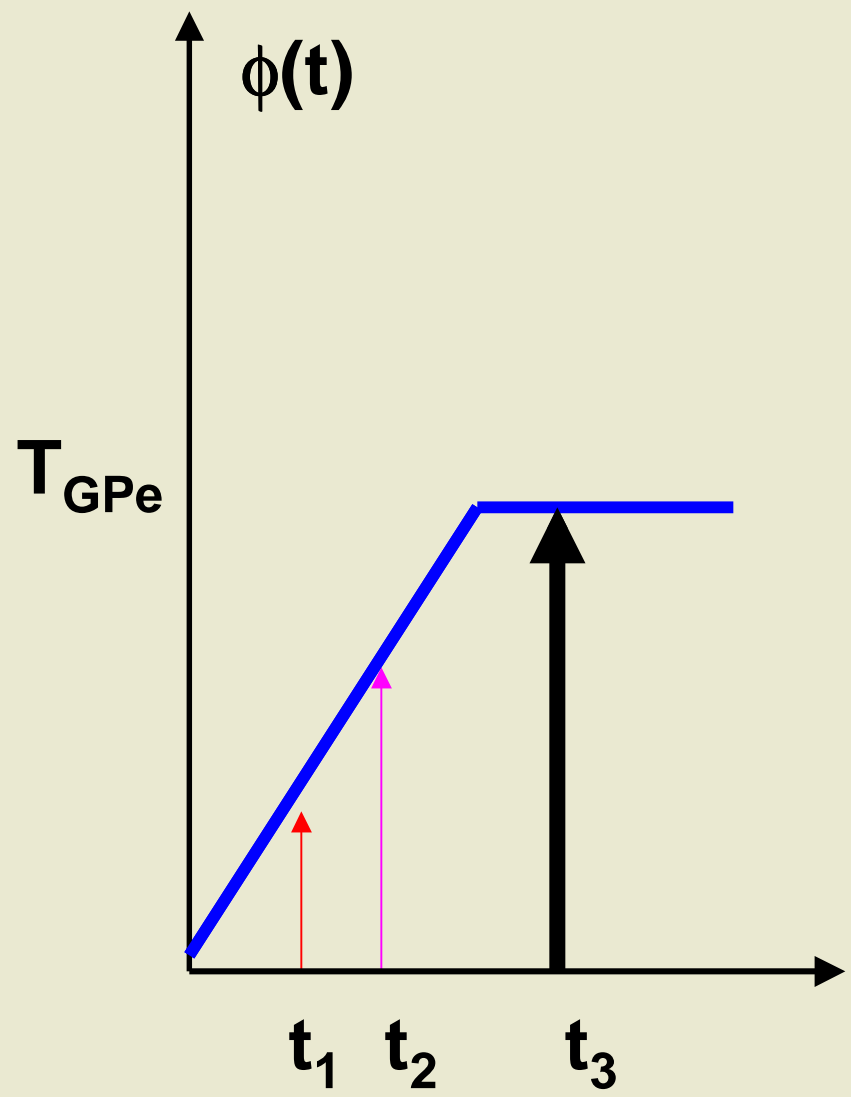
# Phase Response Curve



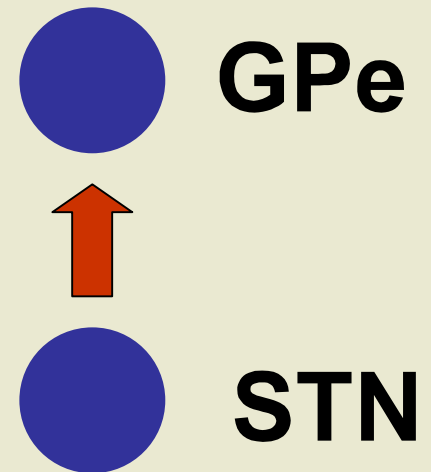
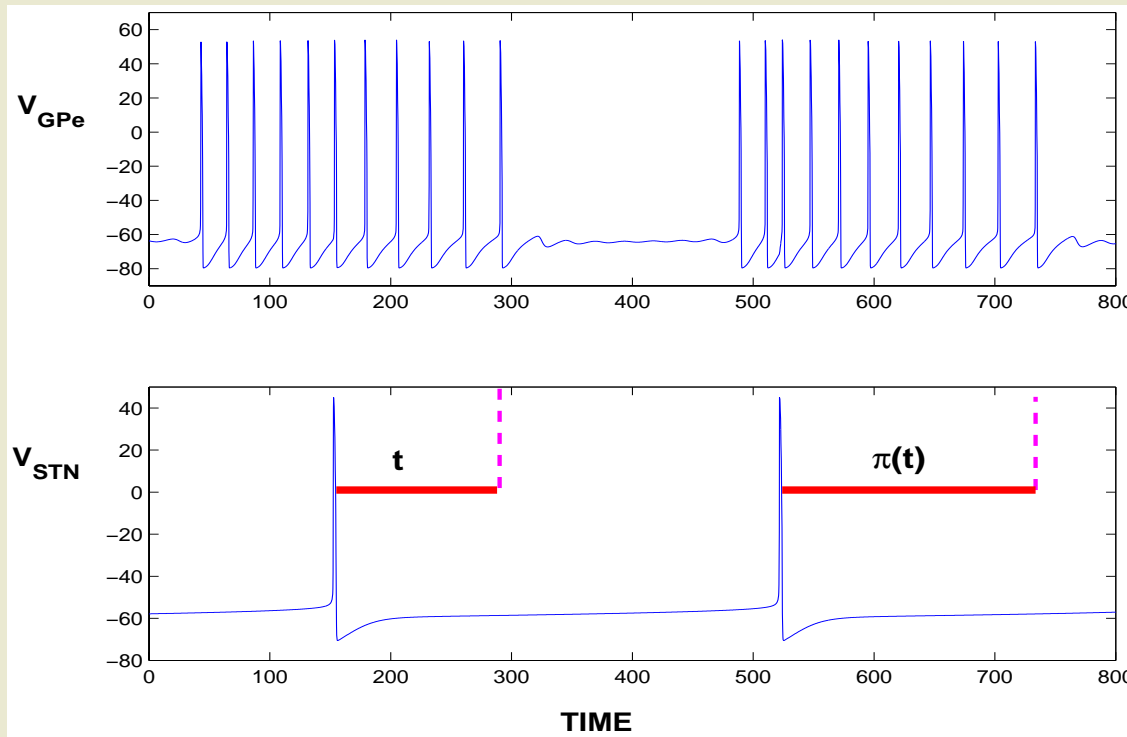
# Phase Response Curve



# Phase Response Curve



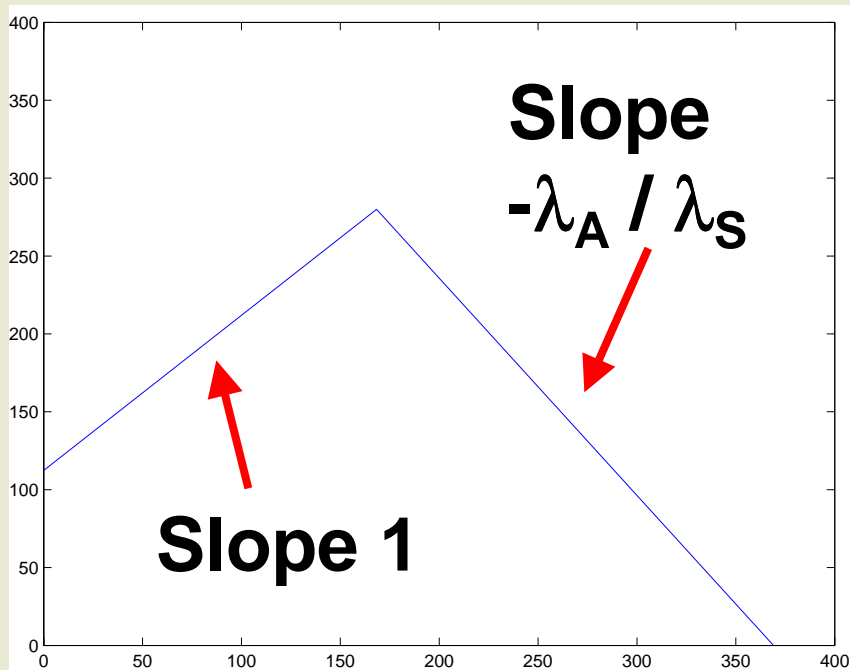
# One Dimensional Map



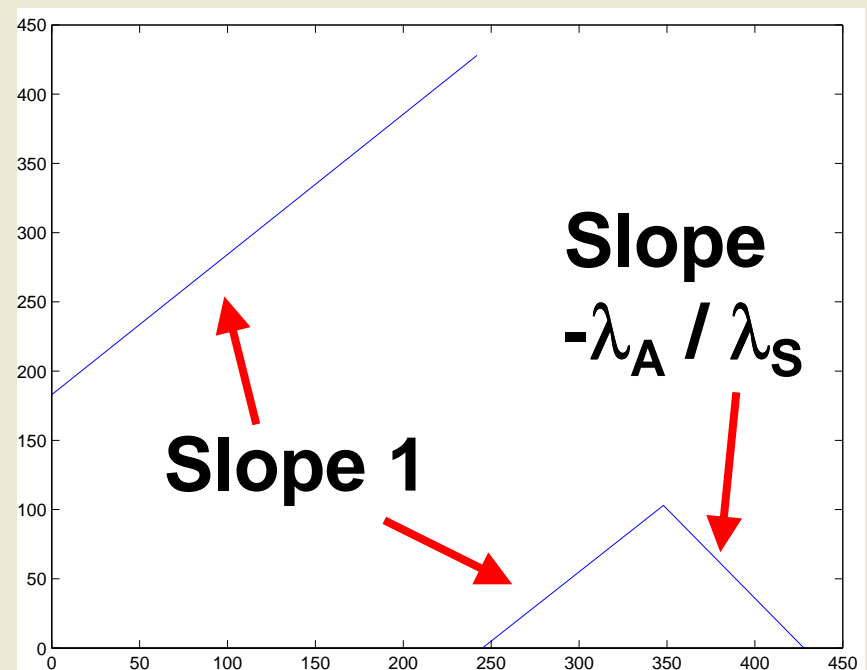
- $t$  = time from STN firing to fall-down of GPe cell
- $\pi(t)$  = time of next GPe fall-down since STN firing

# Linear Approximation of Map

$$T_{GPe} > T_{STN}$$

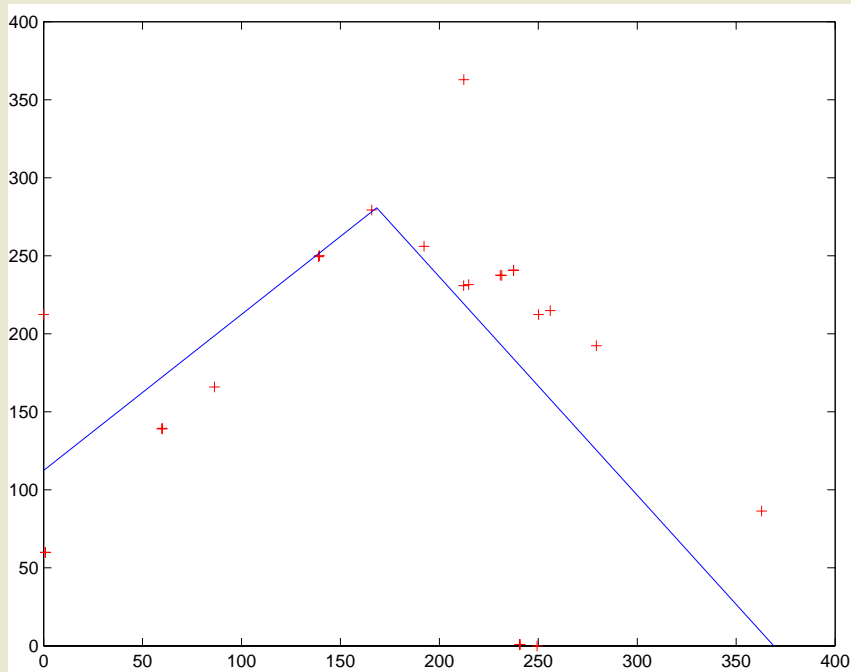


$$T_{GPe} < T_{STN}$$

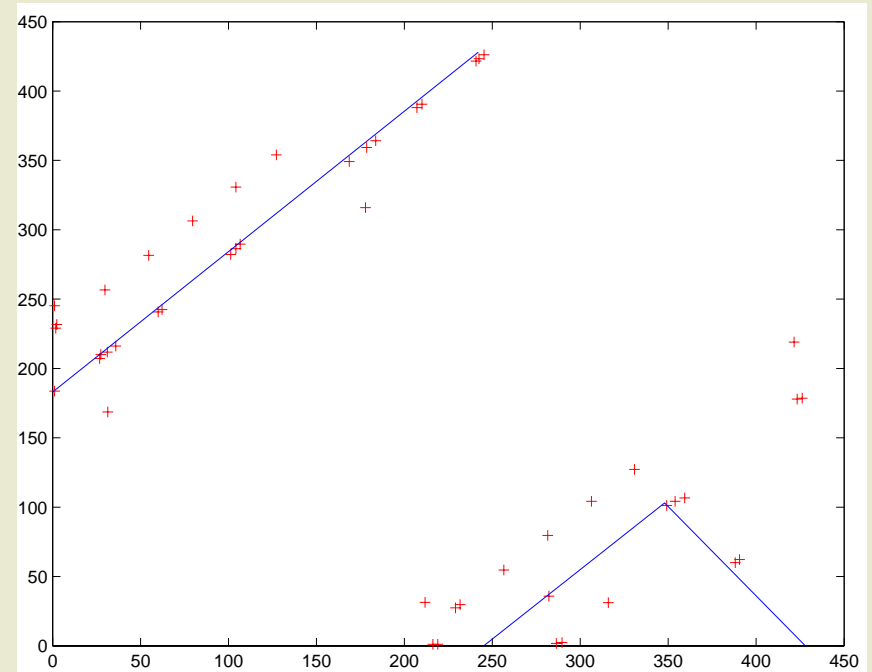


# Numerically Computed Map

$$T_{GPe} > T_{STN}$$



$$T_{GPe} < T_{STN}$$

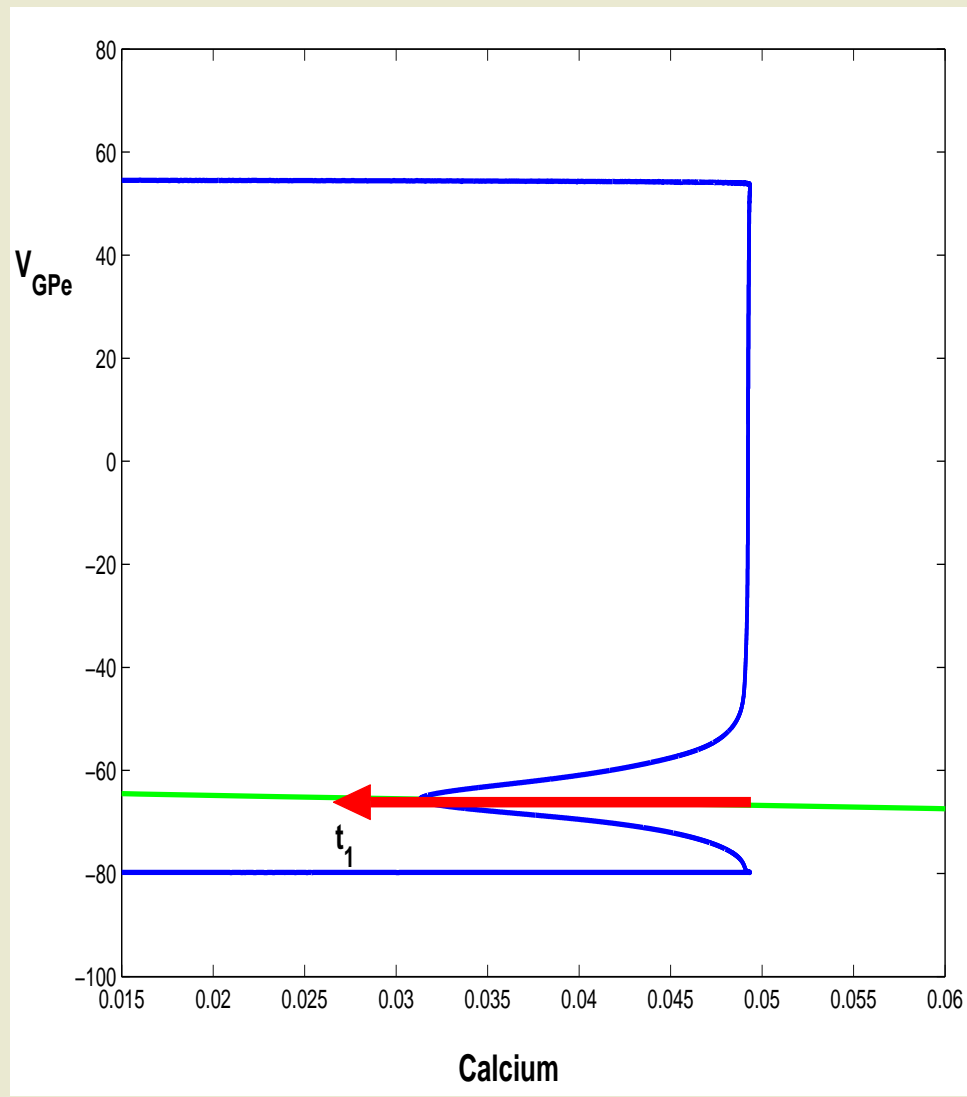
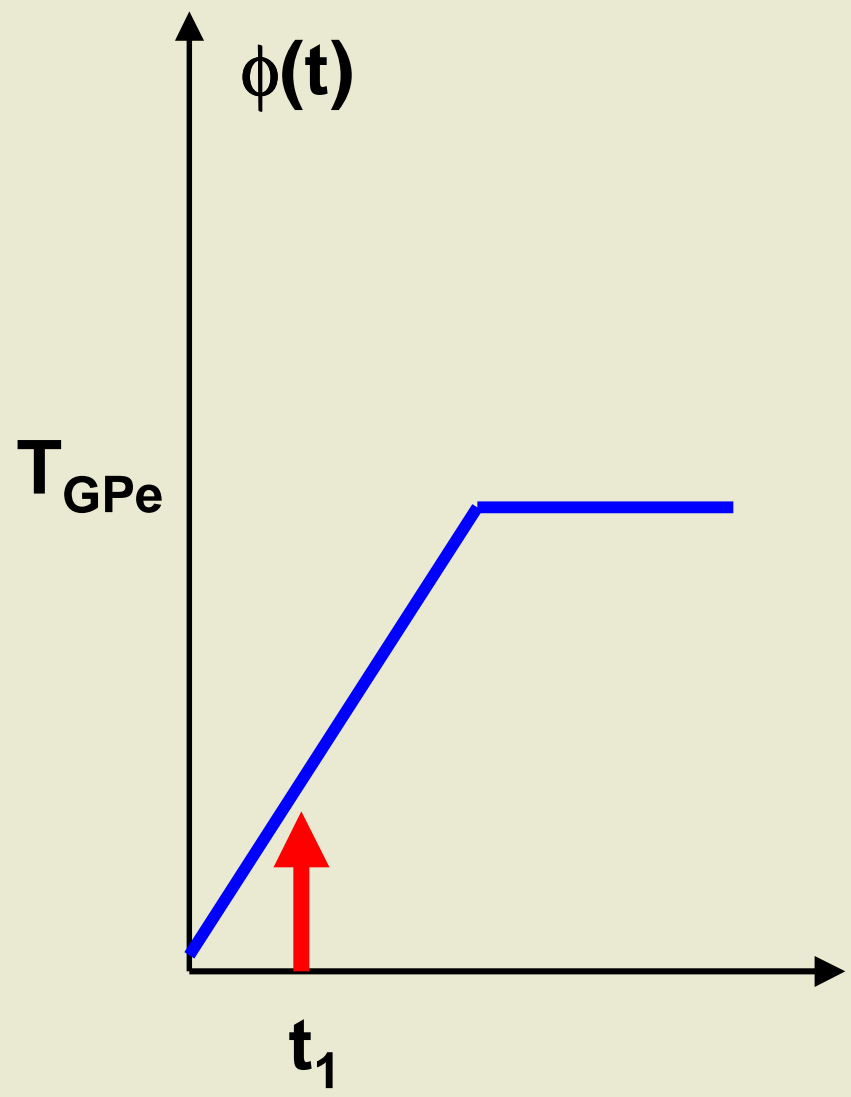




# SUMMARY

- **STN/GPe Network Exhibits Both Irregular and Synchronous Rhythmic Activity**
- **STN Cells show Reverse Spike Adaptation that May Increase Correlations**
- **Transition Between Irregular and Rhythmic Patterns May Arise from Changes in Rebound Properties of STN Cells**
- **Dynamics of Irregular and Clustered Rhythms can be analyzed using lower-dimensional maps**

# Phase Response Curve



# Phase Response Curve

