## Multiplicities of graded families of linear series

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We give simple necessary and sufficient conditions on projective schemes over a field k for asymptotic limits of the growth of all graded linear series of a fixed Kodaira-Iitaka dimension to exist. We begin by defining the volume of line bundles and graded linear series, cover some interesting properties, and discuss methods for computing it.